## DOCUMENT CHANGE HISTORY

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PREFACE

WHAT IS THIS DOCUMENT?

This Best Practices Guide is a manual to help developers obtain the best performance from the NVIDIA® CUDA™ architecture using version 4.1 of the CUDA Toolkit. It presents established parallelization and optimization techniques and explains coding metaphors and idioms that can greatly simplify programming for the CUDA architecture.

While the contents can be used as a reference manual, you should be aware that some topics are revisited in different contexts as various programming and configuration topics are explored. As a result, it is recommended that first-time readers proceed through the guide sequentially. This approach will greatly improve your understanding of effective programming practices and enable you to better use the guide for reference later.

WHO SHOULD READ THIS GUIDE?

The discussions in this guide all use the C programming language, so you should be comfortable reading C code.

This guide refers to and relies on several other documents that you should have at your disposal for reference, all of which are available at no cost from the CUDA website http://developer.nvidia.com/cuda-downloads. The following documents are especially important resources:

► CUDA Getting Started Guide
► CUDA C Programming Guide
In particular, the optimization section of this guide assumes that you have already successfully downloaded and installed the CUDA Toolkit (if not, please refer to the relevant CUDA Getting Started Guide for your platform) and that you have a basic familiarity with the CUDA C programming language and environment (if not, please refer to the CUDA C Programming Guide).

**ASSESS, PARALLELIZE, OPTIMIZE, DEPLOY**

This guide introduces the *Assess, Parallelize, Optimize, Deploy* ("APOD") design cycle for applications with the goal of helping application developers to rapidly identify the portions of their code that would most readily benefit from GPU acceleration, rapidly realize that benefit, and begin leveraging the resulting speedups in production as early as possible.

APOD is a cyclical process: initial speedups can be achieved, tested, and deployed with only minimal initial investment of time, at which point the cycle can begin again by identifying further optimization opportunities, seeing additional speedups, and then deploying the even faster versions of the application into production.
Assess

For an existing project, the first step is to assess the application to locate the parts of the code that are responsible for the bulk of the execution time. Armed with this knowledge, the developer can evaluate these bottlenecks for parallelization and start to investigate GPU acceleration.

By understanding the end-user’s requirements and constraints and by applying Amdahl’s and Gustafson’s laws, the developer can determine the upper bound of performance improvement from acceleration of the identified portions of the application.

Parallelize

Having identified the hotspots and having done the basic exercises to set goals and expectations, the developer needs to parallelize the code. Depending on the original code, this can be as simple as calling into an existing GPU-optimized library such as cuBLAS, cuFFT, or Thrust, or it could be as simple as adding a few preprocessor directives as hints to a parallelizing compiler.

On the other hand, some applications’ designs will require some amount of refactoring to expose their inherent parallelism. As even future CPU architectures will require exposing this parallelism in order to improve or simply maintain the performance of sequential applications, the CUDA family of parallel programming languages (CUDA C/C++, CUDA Fortran, etc.) aims to make the expression of this parallelism as simple as possible, while simultaneously enabling operation on CUDA-capable GPUs designed for maximum parallel throughput.

Optimize

After each round of application parallelization is complete, the developer can move to optimizing the implementation to improve performance. Since there are many possible optimizations that can be considered, having a good understanding of the needs of the application can help to make the process as smooth as possible. However, as with APOD as a whole, program optimization is an iterative process (identify an opportunity for optimization, apply and test the optimization, verify the speedup achieved, and repeat), meaning that it is not necessary for a programmer to spend large amounts of time memorizing the bulk of all possible optimization strategies prior to seeing good speedups. Instead, strategies can be applied incrementally as they are learned.

Optimizations can be applied at various levels, from overlapping data transfers with computation all the way down to fine-tuning floating-point operation sequences. The available profiling tools are invaluable for guiding this process, as they can help suggest a next-best course of action for the developer’s optimization efforts and provide references into the relevant portions of the optimization section of this guide.
Deploy

Having completed the GPU acceleration of one or more components of the application it is possible to compare the outcome with the original expectation. Recall that the initial assess step allowed the developer to determine an upper bound for the potential speedup attainable by accelerating given hotspots.

Before tackling other hotspots to improve the total speedup, the developer should consider taking the partially parallelized implementation and carry it through to production. This is important for a number of reasons; for example, it allows the user to profit from their investment as early as possible (the speedup may be partial but is still valuable), and it minimizes risk for the developer and the user by providing an evolutionary rather than revolutionary set of changes to the application.

RECOMMENDATIONS AND BEST PRACTICES

Throughout this guide, specific recommendations are made regarding the design and implementation of CUDA C code. These recommendations are categorized by priority, which is a blend of the effect of the recommendation and its scope. Actions that present substantial improvements for most CUDA applications have the highest priority, while small optimizations that affect only very specific situations are given a lower priority.

Before implementing lower priority recommendations, it is good practice to make sure all higher priority recommendations that are relevant have already been applied. This approach will tend to provide the best results for the time invested and will avoid the trap of premature optimization.

The criteria of benefit and scope for establishing priority will vary depending on the nature of the program. In this guide, they represent a typical case. Your code might reflect different priority factors. Regardless of this possibility, it is good practice to verify that no higher-priority recommendations have been overlooked before undertaking lower-priority items.

Code samples throughout the guide omit error checking for conciseness. Production code should, however, systematically check the error code returned by each API call and check for failures in kernel launches by calling cudaGetLastError().
ASSESSING YOUR APPLICATION

From supercomputers to mobile phones, modern processors increasingly rely on parallelism to provide performance. The core computational unit, which includes control, arithmetic, registers and typically some cache, is replicated some number of times and connected to memory via a network. As a result, all modern processors require parallel code in order to achieve good utilization of their computational power.

While processors are evolving to expose more fine-grained parallelism to the programmer, many existing applications have evolved either as serial codes or as coarse-grained parallel codes (for example, where the data is decomposed into regions processed in parallel, with sub-regions shared using MPI). In order to profit from any modern processor architecture, GPUs included, the first steps are to assess the application to identify the hotspots, determine whether they can be parallelized, and understand the relevant workloads both now and in the future.
CUDA programming involves running code on two different platforms concurrently: a host system with one or more CPUs and one or more CUDA-enabled NVIDIA GPU devices.

While NVIDIA GPUs are frequently associated with graphics, they are also powerful arithmetic engines capable of running thousands of lightweight threads in parallel. This capability makes them well suited to computations that can leverage parallel execution. However, the device is based on a distinctly different design from the host system, and it’s important to understand those differences and how they determine the performance of CUDA applications in order to use CUDA effectively.

1.1 DIFFERENCES BETWEEN HOST AND DEVICE

The primary differences are in threading model and in separate physical memories:

- **Threading resources.** Execution pipelines on host systems can support a limited number of concurrent threads. Servers that have four hex-core processors today can run only 24 threads concurrently (or 48 if the CPUs support HyperThreading.) By comparison, the smallest executable unit of parallelism on a CUDA device comprises 32 threads (termed a warp of threads). Modern NVIDIA GPUs can support up to 1536 active threads concurrently per multiprocessor (see Section F.1 of the CUDA C Programming Guide). On GPUs with 16 multiprocessors, this leads to more than 24,000 concurrently active threads.

- **Threads.** Threads on a CPU are generally heavyweight entities. The operating system must swap threads on and off CPU execution channels to provide multithreading capability. Context switches (when two threads are swapped) are
therefore slow and expensive. By comparison, threads on GPUs are extremely lightweight. In a typical system, thousands of threads are queued up for work (in warps of 32 threads each). If the GPU must wait on one warp of threads, it simply begins executing work on another. Because separate registers are allocated to all active threads, no swapping of registers or other state need occur when switching among GPU threads. Resources stay allocated to each thread until it completes its execution. In short, CPU cores are designed to minimize latency for one or two threads at a time each, whereas GPUs are designed to handle a large number of concurrent, lightweight threads in order to maximize throughput.

- **RAM.** The host system and the device each have their own distinct attached physical memories. As the host and device memories are separated by the PCI Express (PCIe) bus, items in the host memory must occasionally be communicated across the bus to the device memory or vice versa as described in Section 1.2.

These are the primary hardware differences between CPU hosts and GPU devices with respect to parallel programming. Other differences are discussed as they arise elsewhere in this document. Applications composed with these differences in mind can treat the host and device together as a cohesive heterogeneous system wherein each processing unit is leveraged to do the kind of work it does best: sequential work on the host and parallel work on the device.

### 1.2 WHAT RUNS ON A CUDA-ENABLED DEVICE?

The following issues should be considered when determining what parts of an application to run on the device:

- The device is ideally suited for computations that can be run on numerous data elements simultaneously in parallel. This typically involves arithmetic on large data sets (such as matrices) where the same operation can be performed across thousands, if not millions, of elements at the same time. This is a requirement for good performance on CUDA: the software must use a large number (generally thousands or tens of thousands) of concurrent threads. The support for running numerous threads in parallel derives from the CUDA architecture’s use of a lightweight threading model described above.

- For best performance, there should be some coherence in memory access by adjacent threads running on the device. Certain memory access patterns enable the hardware to coalesce groups of reads or writes of multiple data items into one operation. Data that cannot be laid out so as to enable coalescing, or that doesn’t have enough locality to use the L1 or texture caches effectively, will tend to see lesser speedups when used in computations on CUDA.
To use CUDA, data values must be transferred from the host to the device along the PCI Express (PCIe) bus. These transfers are costly in terms of performance and should be minimized. (See Section 6.1.) This cost has several ramifications:

- The complexity of operations should justify the cost of moving data to and from the device. Code that transfers data for brief use by a small number of threads will see little or no performance benefit. The ideal scenario is one in which many threads perform a substantial amount of work.

For example, transferring two matrices to the device to perform a matrix addition and then transferring the results back to the host will not realize much performance benefit. The issue here is the number of operations performed per data element transferred. For the preceding procedure, assuming matrices of size \( N \times N \), there are \( N^2 \) operations (additions) and \( 3N^2 \) elements transferred, so the ratio of operations to elements transferred is \( 1:3 \) or \( O(1) \). Performance benefits can be more readily achieved when this ratio is higher. For example, a matrix multiplication of the same matrices requires \( N^3 \) operations (multiply-add), so the ratio of operations to elements transferred is \( O(N) \), in which case the larger the matrix the greater the performance benefit. The types of operations are an additional factor, as additions have different complexity profiles than, for example, trigonometric functions. It is important to include the overhead of transferring data to and from the device in determining whether operations should be performed on the host or on the device.

- Data should be kept on the device as long as possible. Because transfers should be minimized, programs that run multiple kernels on the same data should favor leaving the data on the device between kernel calls, rather than transferring intermediate results to the host and then sending them back to the device for subsequent calculations. So, in the previous example, had the two matrices to be added already been on the device as a result of some previous calculation, or if the results of the addition would be used in some subsequent calculation, the matrix addition should be performed locally on the device. This approach should be used even if one of the steps in a sequence of calculations could be performed faster on the host. Even a relatively slow kernel may be advantageous if it avoids one or more PCIe transfers. Section 6.1 provides further details, including the measurements of bandwidth between the host and the device versus within the device proper.
Chapter 2.
APPLICATION PROFILING

2.1 PROFILE

Many codes accomplish a significant portion of the work with a relatively small amount of code. Using a profiler, the developer can identify such hotspots and start to compile a list of candidates for parallelization.

2.1.1 Creating the Profile

There are many possible approaches to profiling the code, but in all cases the objective is the same: to identify the function or functions in which the application is spending most of its execution time.

High Priority: To maximize developer productivity, profile the application to determine hotspots and bottlenecks.

The most important consideration with any profiling activity is to ensure that the workload is realistic – i.e., that information gained from the test and decisions based upon that information are relevant to real data. Using unrealistic workloads can lead to sub-optimal results and wasted effort both by causing developers to optimize for unrealistic problem sizes and by causing developers to concentrate on the wrong functions.

There are a number of tools that can be used to generate the profile. The following example is based on gprof, which is an open-source profiler for Linux platforms from the GNU Binutils collection.
2.1.2 Identifying Hotspots

In the example above, we can clearly see that the function `genTimeStep()` takes one-third of the total running time of the application. This should be our first candidate function for parallelization. Section 2.1.3 discusses the potential benefit we might expect from such parallelization.

It is worth noting that several of the other functions in the above example also take up a significant portion of the overall running time, such as `calcStats()` and `calcSummaryData()`. Parallelizing these functions as well should increase our speedup potential. However, since APOD is a cyclical process, we might opt to parallelize these functions in a subsequent APOD pass, thereby limiting the scope of our work in any given pass to a smaller set of incremental changes.

2.1.3 Understanding Scaling

The amount of performance benefit an application will realize by running on CUDA depends entirely on the extent to which it can be parallelized. Code that cannot be sufficiently parallelized should run on the host, unless doing so would result in excessive transfers between the host and the device.

**High Priority:** To get the maximum benefit from CUDA, focus first on finding ways to parallelize sequential code.

By understanding how applications can scale it is possible to set expectations and plan an incremental parallelization strategy. Section 2.1.3.1 describes strong scaling, which allows us to set an upper bound for the speedup with a fixed problem size. Section

---

# Application Profiling

```
$ gcc -O2 -g -pg myprog.c
$ gprof ./a.out > profile.txt
```

Each sample counts as 0.01 seconds.

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- genTimeStep
- calcStats
- calcSummaryData
- write
- mcount
- tzset
- tolower
- strlen
- strchr
- main
- memcpy
- printf
- profil
- report
2.1.3.2 describes weak scaling, where the speedup is attained by growing the problem size. In many applications, a combination of strong and weak scaling is desirable.

### 2.1.3.1 Strong scaling and Amdahl’s Law

Strong scaling is a measure of how, for a fixed overall problem size, the time to solution decreases as more processors are added to a system. An application that exhibits linear strong scaling has a speedup equal to the number of processors used.

Strong scaling is usually equated with Amdahl’s Law, which specifies the maximum speedup that can be expected by parallelizing portions of a serial program. Essentially, it states that the maximum speedup $S$ of a program is:

$$ S = \frac{1}{(1 - P) + \frac{P}{N}} $$

Here $P$ is the fraction of the total serial execution time taken by the portion of code that can be parallelized and $N$ is the number of processors over which the parallel portion of the code runs.

The larger $N$ is (that is, the greater the number of processors), the smaller the $P/N$ fraction. It can be simpler to view $N$ as a very large number, which essentially transforms the equation into $S = 1 / (1 - P)$. Now, if $\frac{3}{4}$ of the running time of a sequential program is parallelized, the maximum speedup over serial code is $1 / (1 - \frac{3}{4}) = 4$.

In reality, most applications do not exhibit perfectly linear strong scaling, even if they do exhibit some degree of strong scaling. For most purposes, the key point is that the larger the parallelizable portion $P$ is, the greater the potential speedup. Conversely, if $P$ is a small number (meaning that the application is not substantially parallelizable), increasing the number of processors $N$ does little to improve performance. Therefore, to get the largest speedup for a fixed problem size, it is worthwhile to spend effort on increasing $P$, maximizing the amount of code that can be parallelized.

### 2.1.3.2 Weak scaling and Gustafson’s Law

Weak scaling is a measure of how the time to solution changes as more processors are added to a system with a fixed problem size per processor; i.e., where the overall problem size increases as the number of processors is increased.

Weak scaling is often equated with Gustafson’s Law, which states that in practice, the problem size scales with the number of processors. Because of this, the maximum speedup $S$ of a program is:

$$ S = N + (1 - P)(1 - N) $$
Here $P$ is the fraction of the total serial execution time taken by the portion of code that can be parallelized and $N$ is the number of processors over which the parallel portion of the code runs.

Another way of looking at Gustafson’s Law is that it is not the problem size that remains constant as we scale up the system but rather the execution time. Note that Gustafson’s Law assumes that the ratio of serial to parallel execution remains constant, reflecting additional cost in setting up and handling the larger problem.

### 2.1.3.3 Applying Strong and Weak Scaling

Understanding which type of scaling is most applicable to an application is an important part of estimating speedup. For some applications the problem size will remain constant and hence only strong scaling is applicable. An example would be modeling how two molecules interact with each other, where the molecule sizes are fixed.

For other applications, the problem size will grow to fill the available processors. Examples include modeling fluids or structures as meshes or grids and some Monte Carlo simulations, where increasing the problem size provides increased accuracy.

Having understood the application profile, the developer should understand how the problem size would change if the computational performance changes and then apply either Amdahl’s or Gustafson’s Law to determine an upper bound for the speedup.
PARALLELIZING YOUR APPLICATION

Having identified the hotspots and having done the basic exercises to set goals and expectations, the developer needs to parallelize the code. Depending on the original code, this can be as simple as calling into an existing GPU-optimized library such as cuBLAS, cuFFT, or Thrust, or it could be as simple as adding a few preprocessor directives as hints to a parallelizing compiler.

On the other hand, some applications’ designs will require some amount of refactoring to expose their inherent parallelism. As even future CPU architectures will require exposing this parallelism in order to improve or simply maintain the performance of sequential applications, the CUDA family of parallel programming languages (CUDA C/C++, CUDA Fortran, etc.) aims to make the expression of this parallelism as simple as possible, while simultaneously enabling operation on CUDA-capable GPUs designed for maximum parallel throughput.
Chapter 3.
GETTING STARTED

There are several key strategies for parallelizing sequential code. While the details of how to apply these strategies to a particular application is a complex and problem-specific topic, the general themes listed here apply regardless of whether we are parallelizing code to run on for multicore CPUs or for use on CUDA GPUs.

3.1 PARALLEL LIBRARIES

The most straightforward approach to parallelizing an application is to leverage existing libraries that take advantage of parallel architectures on our behalf. The CUDA Toolkit includes a number of such libraries that have been fine-tuned for NVIDIA CUDA GPUs, such as cuBLAS, cuFFT, and so on.

The key here is that libraries are most useful when they match well with the needs of the application. Applications already using other BLAS libraries can often quite easily switch to cuBLAS, for example, whereas applications that do little to no linear algebra will have little use for cuBLAS. The same goes for other CUDA Toolkit libraries: cuFFT has an interface similar to that of FFTW, etc.

Also of note is the Thrust library, which is a parallel C++ template library similar to the C++ Standard Template Library. Thrust provides a rich collection of data parallel primitives such as scan, sort, and reduce, which can be composed together to implement complex algorithms with concise, readable source code. By describing your computation in terms of these high-level abstractions you provide Thrust with the freedom to select the most efficient implementation automatically. As a result, Thrust can be utilized in rapid prototyping of CUDA applications, where programmer productivity matters most, as well as in production, where robustness and absolute performance are crucial.
3.2 PARALLELIZING COMPILERS

Another common approach to parallelization of sequential codes is to make use of parallelizing compilers. Often this means the use of directives-based approaches, where the programmer uses a pragma or other similar notation to provide hints to the compiler about where parallelism can be found without needing to modify or adapt the underlying code itself. By exposing parallelism to the compiler, directives allow the compiler to do the detailed work of mapping the computation onto the parallel architecture.

The OpenACC standard provides a set of compiler directives to specify loops and regions of code in standard C, C++ and Fortran that should be offloaded from a host CPU to an attached accelerator such as a CUDA GPU. The details of managing the accelerator device are handled implicitly by an OpenACC-enabled compiler and runtime.


3.3 CODING TO EXPOSE PARALLELISM

For applications that need additional functionality or performance beyond what existing parallel libraries or parallelizing compilers can provide, parallel programming languages such as CUDA C/C++ that integrate seamlessly with existing sequential code are essential.

Once we have located a hotspot in our application’s profile assessment and determined that custom code is the best approach, we can use CUDA C/C++ to expose the parallelism in that portion of our code as a CUDA kernel. We can then launch this kernel onto the GPU and retrieve the results without requiring major rewrites to the rest of our application.

This approach is most straightforward when the majority of the total running time of our application is spent in a few relatively isolated portions of the code. More difficult to parallelize are applications with a very flat profile – i.e., applications where the time spent is spread out relatively evenly across a wide portion of the code base. For the latter variety of application, some degree of code refactoring to expose the inherent parallelism in the application might be necessary, but keep in mind that this refactoring work will tend to benefit all future architectures, CPU and GPU alike, so it is well worth the effort should it become necessary.
Obtaining the right answer is clearly the principal goal of all computation. On parallel systems, it is possible to run into difficulties not typically found in traditional serial-oriented programming. These include threading issues, unexpected values due to the way floating-point values are computed, and challenges arising from differences in the way CPU and GPU processors operate. This chapter examines issues that can affect the correctness of returned data and points to appropriate solutions.

4.1 VERIFICATION

4.1.1 Reference Comparison

A key aspect of correctness verification for modifications to any existing program is to establish some mechanism whereby previous known-good reference outputs from representative inputs can be compared to new results. After each change is made, ensure that the results match using whatever criteria apply to the particular algorithm. Some will expect bitwise identical results, which is not always possible, especially where floating-point arithmetic is concerned; see Section 4.3 regarding numerical accuracy. For other algorithms, implementations may be considered correct if they match the reference within some small epsilon.

Note that the process used for validating numerical results can easily be extended to validate performance results as well. We want to ensure that each change we make is correct and that it improves performance (and by how much). Checking these things frequently as an integral part of our cyclical APOD process will help ensure that we achieve the desired results as rapidly as possible.
4.1.2 Unit Testing

A useful counterpart to the reference comparisons described above is to structure the code itself in such a way that is readily verifiable at the unit level. For example, we can write our CUDA kernels as a collection of many short _device_ functions rather than one large monolithic _global_ function; each device function can be tested independently before hooking them all together.

For example, many kernels have complex addressing logic for accessing memory in addition to their actual computation. If we validate our addressing logic separately prior to introducing the bulk of the computation, then this will simplify any later debugging efforts. (Note that the CUDA compiler considers any device code that does not contribute to a write to global memory as dead code subject to elimination, so we must at least write _something_ out to global memory as a result of our addressing logic in order to successfully apply this strategy.)

Going a step further, if most functions are defined as _host_ _device_ rather than just _device_ functions, then these functions can be tested on both the CPU and the GPU, thereby increasing our confidence that the function is correct and that there will not be any unexpected differences in the results. If there _are_ differences, then those differences will be seen early and can be understood in the context of a simple function.

As a useful side effect, this strategy will allow us a means to reduce code duplication should we wish to include both CPU and GPU execution paths in our application: if the bulk of the work of our CUDA kernels is done in _host_ _device_ functions, we can easily call those functions from both the host code _and_ the device code without duplication.

4.2 DEBUGGING


4.3 NUMERICAL ACCURACY AND PRECISION

Incorrect or unexpected results arise principally from issues of floating-point accuracy due to the way floating-point values are computed and stored. The following sections explain the principal items of interest. Other peculiarities of floating-point arithmetic are presented in Section F.2 of the CUDA C Programming Guide as well as in a whitepaper and accompanying webinar on floating-point precision and performance available from http://developer.nvidia.com/content/precision-performance-floating-point-and-ieee-754-compliance-nvidia-gpus.

4.3.1 Single vs. Double Precision

Devices of compute capability 1.3 and higher provide native support for double-precision floating-point values (that is, values 64 bits wide). Results obtained using double-precision arithmetic will frequently differ from the same operation performed via single-precision arithmetic due to the greater precision of the former and due to rounding issues. Therefore, it is important to be sure to compare like with like and to express the results within a certain tolerance rather than expecting them to be exact.

Whenever doubles are used, use at least the -arch=sm_13 switch on the nvcc command line; see Sections 3.1.3 and 3.1.4 of the CUDA C Programming Guide for more details.

4.3.2 Floating-Point Math Is Not Associative

Each floating-point arithmetic operation involves a certain amount of rounding. Consequently, the order in which arithmetic operations are performed is important. If A, B, and C are floating-point values, (A+B)+C is not guaranteed to equal A+(B+C) as it is in symbolic math. When you parallelize computations, you potentially change the order of operations and therefore the parallel results might not match sequential results. This limitation is not specific to CUDA, but an inherent part of parallel computation on floating-point values.

4.3.3 Promotions to Doubles and Truncations to Floats

When comparing the results of computations of float variables between the host and device, make sure that promotions to double precision on the host do not account for different numerical results. For example, if the code segment

```c
float a;
...
a = a*1.02;
```

were performed on a device of compute capability 1.2 or less, or on a device with compute capability 1.3 but compiled without enabling double precision (as mentioned
above), then the multiplication would be performed in single precision. However, if the code were performed on the host, the literal 1.02 would be interpreted as a double-precision quantity and a would be promoted to a double, the multiplication would be performed in double precision, and the result would be truncated to a float—thereby yielding a slightly different result. If, however, the literal 1.02 were replaced with 1.02f, the result would be the same in all cases because no promotion to doubles would occur. To ensure that computations use single-precision arithmetic, always use float literals.

In addition to accuracy, the conversion between doubles and floats (and vice versa) has a detrimental effect on performance, as discussed in Chapter 8.

### 4.3.4 IEEE 754 Compliance

All CUDA compute devices follow the IEEE 754 standard for binary floating-point representation, with some small exceptions. These exceptions, which are detailed in Section F.2 of the *CUDA C Programming Guide*, can lead to results that differ from IEEE 754 values computed on the host system.

One of the key differences is the fused multiply-add (FMA) instruction, which combines multiply-add operations into a single instruction execution. Its result will often differ slightly from results obtained by doing the two operations separately.

### 4.3.5 x86 80-bit Computations

x86 processors can use an 80-bit “double extended precision” math when performing floating-point calculations. The results of these calculations can frequently differ from pure 64-bit operations performed on the CUDA device. To get a closer match between values, set the x86 host processor to use regular double or single precision (64 bits and 32 bits, respectively). This is done with the `FLDCW` assembly instruction or the equivalent operating system API.
After each round of application parallelization is complete, the developer can move to optimizing the implementation to improve performance. Since there are many possible optimizations that can be considered, having a good understanding of the needs of the application can help to make the process as smooth as possible. However, as with APOD as a whole, program optimization is an iterative process (identify an opportunity for optimization, apply and test the optimization, verify the speedup achieved, and repeat), meaning that it is not necessary for a programmer to spend large amounts of time memorizing the bulk of all possible optimization strategies prior to seeing good speedups. Instead, strategies can be applied incrementally as they are learned.

Optimizations can be applied at various levels, from overlapping data transfers with computation all the way down to fine-tuning floating-point operation sequences. The available profiling tools are invaluable for guiding this process, as they can help suggest a next-best course of action for the developer’s optimization efforts and provide references into the relevant portions of the optimization section of this guide.
Chapter 5.
PERFORMANCE METRICS

When attempting to optimize CUDA code, it pays to know how to measure performance accurately and to understand the role that bandwidth plays in performance measurement. This chapter discusses how to correctly measure performance using CPU timers and CUDA events. It then explores how bandwidth affects performance metrics and how to mitigate some of the challenges it poses.

5.1 TIMING

CUDA calls and kernel executions can be timed using either CPU or GPU timers. This section examines the functionality, advantages, and pitfalls of both approaches.

5.1.1 Using CPU Timers

Any CPU timer can be used to measure the elapsed time of a CUDA call or kernel execution. The details of various CPU timing approaches are outside the scope of this document, but developers should always be aware of the resolution their timing calls provide.

When using CPU timers, it is critical to remember that many CUDA API functions are asynchronous; that is, they return control back to the calling CPU thread prior to completing their work. All kernel launches are asynchronous, as are memory-copy functions with the Async suffix on their names. Therefore, to accurately measure the elapsed time for a particular call or sequence of CUDA calls, it is necessary to synchronize the CPU thread with the GPU by calling cudaDeviceSynchronize() immediately before starting and stopping the CPU timer.
cudaDeviceSynchronize() blocks the calling CPU thread until all CUDA calls previously issued by the thread are completed.

Although it is also possible to synchronize the CPU thread with a particular stream or event on the GPU, these synchronization functions are not suitable for timing code in streams other than the default stream. cudaStreamSynchronize() blocks the CPU thread until all CUDA calls previously issued into the given stream have completed.

cudaEventSynchronize() blocks until a given event in a particular stream has been recorded by the GPU. Because the driver may interleave execution of CUDA calls from other non-default streams, calls in other streams may be included in the timing.

Because the default stream, stream 0, exhibits serializing behavior for work on the device (an operation in the default stream can begin only after all preceding calls in any stream have completed; and no subsequent operation in any stream can begin until it finishes), these functions can be used reliably for timing in the default stream.

Be aware that CPU-to-GPU synchronization points such as those mentioned in this section imply a stall in the GPU’s processing pipeline and should thus be used sparingly to minimize their performance impact.

### 5.1.2 Using CUDA GPU Timers

The CUDA event API provides calls that create and destroy events, record events (via timestamp), and convert timestamp differences into a floating-point value in milliseconds. Listing 5.1 illustrates their use.

```c
cudaEvent_t start, stop;
float time;

cudaEventCreate(&start);
cudaEventCreate(&stop);

cudaEventRecord( start, 0 );
kernel<<<grid,threads>>>( d_odata, d_idata, size_x, size_y,
NUM_REPS);
cudaEventRecord( stop, 0 );
cudaEventSynchronize( stop );

cudaEventElapsedTime( &time, start, stop );
cudaEventDestroy( start );
cudaEventDestroy( stop );
```

Listing 5.1  How to time code using CUDA events

Here cudaEventRecord() is used to place the start and stop events into the default stream, stream 0. The device will record a timestamp for the event when it reaches that event in the stream. The cudaEventElapsedTime() function returns the time elapsed between the recording of the start and stop events. This value is expressed in
milliseconds and has a resolution of approximately half a microsecond. Like the other calls in this listing, their specific operation, parameters, and return values are described in the CUDA Toolkit Reference Manual. Note that the timings are measured on the GPU clock, so the timing resolution is operating-system-independent.

5.2 BANDWIDTH

Bandwidth—the rate at which data can be transferred—is one of the most important gating factors for performance. Almost all changes to code should be made in the context of how they affect bandwidth. As described in Chapter 6 of this guide, bandwidth can be dramatically affected by the choice of memory in which data is stored, how the data is laid out and the order in which it is accessed, as well as other factors.

To measure performance accurately, it is useful to calculate theoretical and effective bandwidth. When the latter is much lower than the former, design or implementation details are likely to reduce bandwidth, and it should be the primary goal of subsequent optimization efforts to increase it.

**High Priority:** Use the effective bandwidth of your computation as a metric when measuring performance and optimization benefits.

5.2.1 Theoretical Bandwidth Calculation

Theoretical bandwidth can be calculated using hardware specifications available in the product literature. For example, the NVIDIA Tesla M2090 uses GDDR5 (double data rate) RAM with a memory clock rate of 1.85 GHz and a 384-bit-wide memory interface.

Using these data items, the peak theoretical memory bandwidth of the NVIDIA Tesla M2090 is 177.6 GB/sec:

\[
(1.85 \times 10^9 \times (384/8) \times 2) / 10^9 = 177.6 \text{ GB/sec}
\]

In this calculation, the memory clock rate is converted in to Hz, multiplied by the interface width (divided by 8, to convert bits to bytes) and multiplied by 2 due to the double data rate. Finally, this product is divided by \(10^9\) to convert the result to GB/s.

Note that some calculations use 1024\(^3\) instead of \(10^9\) for the final calculation. In such a case, the bandwidth would be 165.4 GB/s. It is important to use the same divisor when calculating theoretical and effective bandwidth so that the comparison is valid.

5.2.2 Effective Bandwidth Calculation

Effective bandwidth is calculated by timing specific program activities and by knowing how data is accessed by the program. To do so, use this equation:
Effective bandwidth \(= \frac{(B_r + B_w)}{10^9} \times \text{time}\)

Here, the effective bandwidth is in units of GB/s, \(B_r\) is the number of bytes read per kernel, \(B_w\) is the number of bytes written per kernel, and time is given in seconds.

For example, to compute the effective bandwidth of a 2048 x 2048 matrix copy, the following formula could be used:

\[
\text{Effective bandwidth} = \frac{(2048^2 \times 4 \times 2)}{10^9} / \text{time}
\]

The number of elements is multiplied by the size of each element (4 bytes for a float), multiplied by 2 (because of the read and write), divided by \(10^9\) (or \(1,024^3\)) to obtain GB of memory transferred. This number is divided by the time in seconds to obtain GB/s.

### 5.2.3 Throughput Reported by Visual Profiler

For devices with compute capability of 2.0 or greater, the Visual Profiler can be used to collect several different memory throughput measures. The following throughput metrics can be displayed in the Details or Detail Graphs view:

- Requested Global Load Throughput
- Requested Global Store Throughput
- Global Load Throughput
- Global Store Throughput
- DRAM Read Throughput
- DRAM Write Throughput

The Requested Global Load Throughput and Requested Global Store Throughput values indicate the global memory throughput requested by the kernel and therefore correspond to the effective bandwidth obtained by the calculation shown under Effective Bandwidth Calculation.

Because the minimum memory transaction size is larger than most word sizes, the actual memory throughput required for a kernel can include the transfer of data not used by the kernel. For global memory accesses, this actual throughput is reported by the Global Load Throughput and Global Store Throughput values.

It’s important to note that both numbers are useful. The actual memory throughput shows how close the code is to the hardware limit, and a comparison of the effective or requested bandwidth to the actual bandwidth presents a good estimate of how much bandwidth is wasted by suboptimal coalescing of memory accesses (see Section 6.2.1). For global memory accesses, this comparison of requested memory bandwidth to actual memory bandwidth is reported by the Global Memory Load Efficiency and Global Memory Store Efficiency metrics.

Note: the Visual Profiler uses \(1024^3\) when converting bytes/sec to GB/sec.
Memory optimizations are the most important area for performance. The goal is to maximize the use of the hardware by maximizing bandwidth. Bandwidth is best served by using as much fast memory and as little slow-access memory as possible. This chapter discusses the various kinds of memory on the host and device and how best to set up data items to use the memory effectively.

6.1 DATA TRANSFER BETWEEN HOST AND DEVICE

The peak theoretical bandwidth between the device memory and the GPU is much higher (177.6 GB/s on the NVIDIA Tesla M2090, for example) than the peak theoretical bandwidth between host memory and device memory (8 GB/s on the PCIe ×16 Gen2). Hence, for best overall application performance, it is important to minimize data transfer between the host and the device, even if that means running kernels on the GPU that do not demonstrate any speedup compared with running them on the host CPU.

High Priority: Minimize data transfer between the host and the device, even if it means running some kernels on the device that do not show performance gains when compared with running them on the host CPU.

Intermediate data structures should be created in device memory, operated on by the device, and destroyed without ever being mapped by the host or copied to host memory.

Also, because of the overhead associated with each transfer, batching many small transfers into one larger transfer performs significantly better than making each transfer separately.
Finally, higher bandwidth between the host and the device is achieved when using page-locked (or pinned) memory, as discussed in the CUDA C Programming Guide and Section 6.1.1 of this document.

6.1.1 Pinned Memory

Page-locked or pinned memory transfers attain the highest bandwidth between the host and the device. On PCIe ×16 Gen2 cards, for example, pinned memory can attain greater than 5 GB/s transfer rates.

Pinned memory is allocated using the cudaHostAlloc() functions in the Runtime API. The bandwidthTest.cu program in the NVIDIA GPU Computing SDK shows how to use these functions as well as how to measure memory transfer performance.

Pinned memory should not be overused. Excessive use can reduce overall system performance because pinned memory is a scarce resource. How much is too much is difficult to tell in advance, so as with all optimizations, test the applications and the systems they run on for optimal performance parameters.

6.1.2 Asynchronous Transfers and Overlapping Transfers with Computation

Data transfers between the host and the device using cudaMemcpy() are blocking transfers; that is, control is returned to the host thread only after the data transfer is complete. The cudaMemcpyAsync() function is a non-blocking variant of cudaMemcpy() in which control is returned immediately to the host thread. In contrast with cudaMemcpy(), the asynchronous transfer version requires pinned host memory (see Section 6.1.1), and it contains an additional argument, a stream ID. A stream is simply a sequence of operations that are performed in order on the device. Operations in different streams can be interleaved and in some cases overlapped—a property that can be used to hide data transfers between the host and the device.

Asynchronous transfers enable overlap of data transfers with computation in two different ways. On all CUDA-enabled devices, it is possible to overlap host computation with asynchronous data transfers and with device computations. For example, Listing 6.1 demonstrates how host computation in the routine cpuFunction() is performed while data is transferred to the device and a kernel using the device is executed.

```c
  cudaMemcpyAsync(a_d, a_h, size, cudaMemcpyHostToDevice, 0);
  kernel<<<grid, block>>>(a_d);
  cpuFunction();
```

Listing 6.1 Overlapping computation and data transfers

The last argument to the cudaMemcpyAsync() function is the stream ID, which in this case uses the default stream, stream 0. The kernel also uses the default stream, and it will not
begin execution until the memory copy completes; therefore, no explicit synchronization is needed. Because the memory copy and the kernel both return control to the host immediately, the host function `cpuFunction()` overlaps their execution.

In Listing 6.1, the memory copy and kernel execution occur sequentially. On devices that are capable of concurrent copy and compute, it is possible to overlap kernel execution on the device with data transfers between the host and the device. Whether a device has this capability is indicated by the `deviceOverlap` field of the `cudaDeviceProp` structure (or listed in the output of the `deviceQuery` SDK sample). On devices that have this capability, the overlap once again requires pinned host memory, and, in addition, the data transfer and kernel must use different, non-default streams (streams with non-zero stream IDs). Non-default streams are required for this overlap because memory copy, memory set functions, and kernel calls that use the default stream begin only after all preceding calls on the device (in any stream) have completed, and no operation on the device (in any stream) commences until they are finished.

Listing 6.2 illustrates the basic technique.

```c
cudaStreamCreate(&stream1);
cudaStreamCreate(&stream2);
ccudaMemcpyAsync(a_d, a_h, size, cudaMemcpyHostToDevice, stream1);
kern<<<grid, block, 0, stream2>>> (otherData_d);
```

**Listing 6.2 Concurrent copy and execute**

In this code, two streams are created and used in the data transfer and kernel executions as specified in the last arguments of the `cudaMemcpyAsync` call and the kernel’s execution configuration.

Listing 6.2 demonstrates how to overlap kernel execution with asynchronous data transfer. This technique could be used when the data dependency is such that the data can be broken into chunks and transferred in multiple stages, launching multiple kernels to operate on each chunk as it arrives. Listing 6.3 and Listing 6.4 demonstrate this. They produce equivalent results. The first segment shows the reference sequential implementation, which transfers and operates on an array of N floats (where N is assumed to be evenly divisible by nThreads).

```c
cudaMemcpy(a_d, a_h, N*sizeof(float), dir);
kern<<<N/nThreads, nThreads>>> (a_d);
```

**Listing 6.3 Sequential copy and execute**

```c
size=N*sizeof(float)/nStreams;
```
for (i=0; i<nStreams; i++) {
    offset = i*N/nStreams;
    cudaMemcpyAsync(a_d+offset, a_h+offset, size, dir, stream[i]);
    kernel<<<N/(nThreads*nStreams), nThreads, 0, stream[i]>>>(a_d+offset);
}

Listing 6.4 shows how the transfer and kernel execution can be broken up into nStreams stages. This approach permits some overlapping of the data transfer and execution.

size=N*sizeof(float)/nStreams;
for (i=0; i<nStreams; i++) {
    offset = i*N/nStreams;
    cudaMemcpyAsync(a_d+offset, a_h+offset, size, dir, stream[i]);
    kernel<<<N/(nThreads*nStreams), nThreads, 0, stream[i]>>>(a_d+offset);
}

Listing 6.4  Staged concurrent copy and execute

(In Listing 6.4, it is assumed that N is evenly divisible by nThreads*nStreams.) Because execution within a stream occurs sequentially, none of the kernels will launch until the data transfers in their respective streams complete. Current GPUs can simultaneously process asynchronous data transfers and execute kernels. GPUs with a single copy engine can perform one asynchronous data transfer and execute kernels whereas GPUs with two copy engines can simultaneously perform one asynchronous data transfer from the host to the device, one asynchronous data transfer from the device to the host, and execute kernels. The number of copy engines on a GPU is given by the asyncEngineCount field of the cudaDeviceProp structure, which is also listed in the output of the deviceQuery SDK sample. (It should be mentioned that it is not possible to overlap a blocking transfer with an asynchronous transfer, because the blocking transfer occurs in the default stream, so it will not begin until all previous CUDA calls complete. It will not allow any other CUDA call to begin until it has completed.) A diagram depicting the timeline of execution for the two code segments is shown in Figure 6.1, and nStreams is equal to 4 for Listing 6.4 in the bottom half of the figure.
Figure 6.1 Timeline comparison for sequential (top) and concurrent (bottom) copy and kernel execution

For this example, it is assumed that the data transfer and kernel execution times are comparable. In such cases, and when the execution time \( t_E \) exceeds the transfer time \( t_T \), a rough estimate for the overall time is \( t_E + t_T/n\text{Streams} \) for the staged version versus \( t_E + t_T \) for the sequential version. If the transfer time exceeds the execution time, a rough estimate for the overall time is \( t_T + t_E/n\text{Streams} \).

### 6.1.3 Zero Copy

Zero copy is a feature that was added in version 2.2 of the CUDA Toolkit. It enables GPU threads to directly access host memory. For this purpose, it requires mapped pinned (non-pageable) memory. On integrated GPUs (i.e., GPUs with the integrated field of the CUDA device properties structure set to 1), mapped pinned memory is always a performance gain because it avoids superfluous copies as integrated GPU and CPU memory are physically the same. On discrete GPUs, mapped pinned memory is advantageous only in certain cases. Because the data is not cached on the GPU, mapped pinned memory should be read or written only once, and the global loads and stores that read and write the memory should be coalesced. Zero copy can be used in place of streams because kernel-originated data transfers automatically overlap kernel execution without the overhead of setting up and determining the optimal number of streams.

#### Low Priority: Use zero-copy operations on integrated GPUs for CUDA Toolkit version 2.2 and later.

The host code in Listing 6.5 shows how zero copy is typically set up.

```c
float *a_h, *a_map;
...
cudaGetDeviceProperties(&prop, 0);
if (!prop.canMapHostMemory)
exit(0);
cudaSetDeviceFlags(cudaDeviceMapHost);
cudaHostAlloc(&a_h, nBytes, cudaHostAllocMapped);
cudaHostGetDevicePointer(&a_map, a_h, 0);
kernelsize, blockSize>>>(a_map);
```

#### Listing 6.5 Zero-copy host code

In this code, the canMapHostMemory field of the structure returned by cudaGetDeviceProperties() is used to check that the device supports mapping host memory to the device’s address space. Page-locked memory mapping is enabled by calling cudaSetDeviceFlags() with cudaDeviceMapHost. Note that cudaSetDeviceFlags() must be called prior to setting a device or making a CUDA call that requires state (that is, essentially, before a context is created). Page-locked mapped host memory is
allocated using `cudaHostAlloc()`, and the pointer to the mapped device address space is obtained via the function `cudaHostGetDevicePointer()`. In the code in Listing 6.5, `kernel()` can reference the mapped pinned host memory using the pointer `a_map` in exactly the same was as it would if `a_map` referred to a location in device memory.

Note: mapped pinned host memory allows you to overlap CPU-GPU memory transfers with computation while avoiding the use of CUDA streams. But since any repeated access to such memory areas causes repeated PCIe transfers, consider creating a second area in device memory to manually cache the previously read host memory data.

### 6.1.4 Unified Virtual Addressing

Devices of compute capability 2.x support a special addressing mode called *Unified Virtual Addressing* (UVA) on 64-bit Linux, MacOS, and Windows XP and on Windows Vista/7 when using TCC driver mode. With UVA, the host memory and the device memories of all installed supported devices share a single virtual address space.

Prior to UVA, an application had to keep track of which pointers referred to device memory (and for which device) and which referred to host memory as a separate bit of metadata (or as hard-coded information in the program) for each pointer. Using UVA, on the other hand, the physical memory space to which a pointer points can be determined simply by inspecting the value of the pointer using `cudaPointerGetAttributes()`.

Under UVA, pinned host memory allocated with `cudaHostAlloc()` will have identical host and device pointers, so it is not necessary to call `cudaHostGetDevicePointer()` for such allocations. Host memory allocations pinned after-the-fact via `cudaHostRegister()`, however, will continue to have different device pointers than their host pointers, so `cudaHostGetDevicePointer()` remains necessary in that case.

UVA is also a necessary precondition for enabling peer-to-peer (P2P) transfer of data directly across the PCIe bus for supported GPUs in supported configurations, bypassing host memory.

See the *CUDA C Programming Guide* for further explanations and software requirements for UVA and P2P.

### 6.2 DEVICE MEMORY SPACES

CUDA devices use several memory spaces, which have different characteristics that reflect their distinct usages in CUDA applications. These memory spaces include global, local, shared, texture, and registers, as shown in Figure 6.2.
Figure 6.2  Memory spaces on a CUDA device

Of these different memory spaces, global memory is the most plentiful; see Section F.1 of the CUDA C Programming Guide for the amounts of memory available in each memory space at each compute capability level. Global, local, and texture memory have the greatest access latency, followed by constant memory, shared memory, and the register file.

The various principal traits of the memory types are shown in Table 6.1.

<table>
<thead>
<tr>
<th>Memory</th>
<th>Location on/off chip</th>
<th>Cached</th>
<th>Access</th>
<th>Scope</th>
<th>Lifetime</th>
</tr>
</thead>
<tbody>
<tr>
<td>Register</td>
<td>On</td>
<td>n/a</td>
<td>R/W</td>
<td>1 thread</td>
<td>Thread</td>
</tr>
<tr>
<td>Local</td>
<td>Off</td>
<td>†</td>
<td>R/W</td>
<td>1 thread</td>
<td>Thread</td>
</tr>
<tr>
<td>Shared</td>
<td>On</td>
<td>n/a</td>
<td>R/W</td>
<td>All threads in block</td>
<td>Block</td>
</tr>
<tr>
<td>Global</td>
<td>Off</td>
<td>†</td>
<td>R/W</td>
<td>All threads + host</td>
<td>Host allocation</td>
</tr>
<tr>
<td>Constant</td>
<td>Off</td>
<td>Yes</td>
<td>R</td>
<td>All threads + host</td>
<td>Host allocation</td>
</tr>
<tr>
<td>Texture</td>
<td>Off</td>
<td>Yes</td>
<td>R</td>
<td>All threads + host</td>
<td>Host allocation</td>
</tr>
</tbody>
</table>

*Cached only on devices of compute capability 2.x.

In the case of texture access, if a texture reference is bound to a linear array in global memory, then the device code can write to the underlying array. Texture references that are bound to CUDA arrays can be written to via surface-write operations by binding a
surface to the same underlying CUDA array storage). Reading from a texture while writing to its underlying global memory array in the same kernel launch should be avoided because the texture caches are read-only and are not invalidated when the associated global memory is modified.

### 6.2.1 Coalesced Access to Global Memory

Perhaps the single most important performance consideration in programming for the CUDA architecture is the coalescing of global memory accesses. Global memory loads and stores by threads of a warp (of a half warp for devices of compute capability 1.x) are coalesced by the device into as few as one transaction when certain access requirements are met.

**High Priority:** Ensure global memory accesses are coalesced whenever possible.

The access requirements for coalescing depend on the compute capability of the device and are documented in the *CUDA C Programming Guide* (Section F.3.2 for compute capability 1.x and Section F.4.2 for compute capability 2.x).

For devices of compute capability 2.x, the requirements can be summarized quite easily: the concurrent accesses of the threads of a warp will coalesce into a number of transactions equal to the number of cache lines necessary to service all of the threads of the warp. By default, all accesses are cached through L1, which as 128-byte lines. For scattered access patterns, to reduce overfetch, it can sometimes be useful to cache only in L2, which caches shorter 32-byte segments (see the *CUDA C Programming Guide*).

Coalescing concepts are illustrated in the following simple examples. These examples assume compute capability 2.x. These examples assume that accesses are cached through L1, which is the default behavior, and that accesses are for 4-byte words, unless otherwise noted.

For corresponding examples for compute capability 1.x, refer to earlier versions of this guide.

#### 6.2.1.1 A Simple Access Pattern

The first and simplest case of coalescing can be achieved by any CUDA-enabled device: the \( k \)-th thread accesses the \( k \)-th word in a cache line. Not all threads need to participate.

For example, if the threads of a warp access adjacent 4-byte words (e.g., adjacent \texttt{float} values), a single 128B L1 cache line and therefore a single coalesced transaction will service that memory access. Such a pattern is shown in Figure 6.3.
Figure 6.3  Coalesced access - all threads access one cache line

This access pattern results in a single 128-byte L1 transaction, indicated by the red rectangle.

If some words of the line had not been requested by any thread (such as if several threads had accessed the same word or if some threads did not participate in the access), all data in the cache line is fetched anyway. Furthermore, if accesses by the threads of the warp had been permuted within this segment, still only one 128-byte L1 transaction would have been performed by a device with compute capability 2.x.

6.2.1.2 A Sequential but Misaligned Access Pattern

If sequential threads in a warp access memory that is sequential but not aligned with the cache lines, two 128-byte L1 cache will be requested, as shown in Figure 6.4.

Figure 6.4  Unaligned sequential addresses that fit into two 128-byte L1-cache lines

For non-caching transactions (i.e., those that bypass L1 and use only the L2 cache), a similar effect is seen, except at the level of the 32-byte L2 segments. In Figure 6.5, we see an example of this: the same access pattern from Figure 6.4 is used, but now L1 caching is disabled, so now five 32-byte L2 segments are needed to satisfy the request.
Memory allocated through the CUDA Runtime API, such as via `cudaMalloc()`, is guaranteed to be aligned to at least 256 bytes. Therefore, choosing sensible thread block sizes, such as multiples of the warp size (i.e., 32 on current GPUs), facilitates memory accesses by warps that are aligned to cache lines. (Consider what would happen to the memory addresses accessed by the second, third, and subsequent thread blocks if the thread block size was not a multiple of warp size, for example.)

### 6.2.1.3 Effects of Misaligned Accesses

It is easy and informative to explore the ramifications of misaligned accesses using a simple copy kernel, such as the one in Listing 6.6.

```c
__global__ void offsetCopy(float *odata, float* idata, int offset)
{
    int xid = blockIdx.x * blockDim.x + threadIdx.x + offset;
    odata[xid] = idata[xid];
}
```

**Listing 6.6** A copy kernel that illustrates misaligned accesses

In Listing 6.6, data is copied from the input array `idata` to the output array, both of which exist in global memory. The kernel is executed within a loop in host code that varies the parameter `offset` from 0 to 32. (Figure 6.4 and Figure 6.5 correspond to misalignments in the cases of caching and non-caching memory accesses, respectively.) The effective bandwidth for the copy with various offsets on an NVIDIA Tesla M2090 (compute capability 2.0, with ECC turned on, as it is by default) is shown in Figure 6.6.
Figure 6.6  Performance of offsetCopy kernel

For the NVIDIA Tesla M2090, global memory accesses with no offset or with offsets that are multiples of 32 words result in a single L1 cache line transaction or 4 L2 cache segment loads (for non-L1-caching loads). The achieved bandwidth is approximately 130GB/s. Otherwise, either two L1 cache lines (caching mode) or four to five L2 cache segments (non-caching mode) are loaded per warp, resulting in approximately 4/5th of the memory throughput achieved with no offsets.

An interesting point is that we might expect the caching case to perform worse than the non-caching case for this sample, given that each warp in the caching case fetches twice as many bytes as it requires, whereas in the non-caching case, only 5/4 as many bytes as required are fetched per warp. In this particular example, that effect is not apparent, however, because adjacent warps reuse the cache lines their neighbors fetched. So while the impact is still evident in the case of caching loads, it is not as great as we might have expected. It would have been more so if adjacent warps had not exhibited such a high degree of reuse of the over-fetched cache lines.

6.2.1.4 Strided Accesses

As seen above, in the case of misaligned sequential accesses, the caches of compute capability 2.x devices help a lot to achieve reasonable performance. It may be different with non-unit-strided accesses, however, and this is a pattern that occurs frequently when dealing with multidimensional data or matrices. For this reason, ensuring that as much as possible of the data in each cache line fetched is actually used is an important part of performance optimization of memory accesses on these devices.
To illustrate the effect of strided access on effective bandwidth, see the kernel
`strideCopy()` in Listing 6.7, which copies data with a stride of `stride` elements between
threads from `idata` to `odata`.

```
__global__ void strideCopy(float *odata, float* idata, int stride)
{
    int xid = (blockIdx.x*blockDim.x + threadIdx.x)*stride;
    odata[xid] = idata[xid];
}
```

**Listing 6.7  A kernel to illustrate non-unit stride data copy**

Figure 6.7 illustrates such a situation; in this case, threads within a warp access words in
memory memory with a stride of 2. This action leads to a load of two L1 cache lines (or
eight L2 cache segments in non-caching mode) per warp on the Tesla M2090 (compute
capability 2.0).

![Adjacent threads accessing memory with a stride of 2](image)

**Figure 6.7  Adjacent threads accessing memory with a stride of 2**

A stride of 2 results in a 50% of load/store efficiency since half the elements in the
transaction are not used and represent wasted bandwidth. As the stride increases, the
effective bandwidth decreases until the point where 32 lines of cache are loaded for the
32 threads in a warp, as indicated in Figure 6.8.
Figure 6.8  Performance of strideCopy kernel

As illustrated in Figure 6.8, non-unit-stride global memory accesses should be avoided whenever possible. One method for doing so utilizes shared memory, which is discussed in the next section.

6.2.2  Shared Memory

Because it is on-chip, shared memory has much higher bandwidth and lower latency than local and global memory—provided there are no bank conflicts between the threads, as detailed in the following section.

6.2.2.1  Shared Memory and Memory Banks

To achieve high memory bandwidth for concurrent accesses, shared memory is divided into equally sized memory modules (banks) that can be accessed simultaneously. Therefore, any memory load or store of \( n \) addresses that spans \( n \) distinct memory banks can be serviced simultaneously, yielding an effective bandwidth that is \( n \) times as high as the bandwidth of a single bank.

However, if multiple addresses of a memory request map to the same memory bank, the accesses are serialized. The hardware splits a memory request that has bank conflicts into as many separate conflict-free requests as necessary, decreasing the effective bandwidth by a factor equal to the number of separate memory requests. The one exception here is when multiple threads in a warp address the same shared memory location, resulting in a broadcast. Devices of compute capability 1.x require all threads of
a half-warp to access the same address in shared memory for broadcast to occur; devices of compute capability 2.x have the additional ability to multicast shared memory accesses (i.e., to send copies of the same value to several but not all threads of the warp).

To minimize bank conflicts, it is important to understand how memory addresses map to memory banks and how to optimally schedule memory requests.

Medium Priority: Accesses to shared memory should be designed to avoid serializing requests due to bank conflicts.

Shared memory banks are organized such that successive 32-bit words are assigned to successive banks and each bank has a bandwidth of 32 bits per clock cycle. The bandwidth of shared memory is 32 bits per bank per clock cycle.

For devices of compute capability 1.x, the warp size is 32 threads and the number of banks is 16. A shared memory request for a warp is split into one request for the first half of the warp and one request for the second half of the warp. Note that no bank conflict occurs if only one memory location per bank is accessed by a half warp of threads.

For devices of compute capability 2.x, the warp size is 32 threads and the number of banks is also 32. A shared memory request for a warp is not split as with devices of compute capability 1.x, meaning that bank conflicts can occur between threads in the first half of a warp and threads in the second half of the same warp (see Section F.4.3 of the CUDA C Programming Guide).

Refer to the CUDA C Programming Guide for more information on how accesses and banks can be matched to avoid conflicts.

6.2.2.2 Shared Memory in Matrix Multiplication (C = AB)

Shared memory enables cooperation between threads in a block. When multiple threads in a block use the same data from global memory, shared memory can be used to access the data from global memory only once. Shared memory can also be used to avoid uncoalesced memory accesses by loading and storing data in a coalesced pattern from global memory and then reordering it in shared memory. Aside from memory bank conflicts, there is no penalty for non-sequential or unaligned accesses by a warp in shared memory.

The use of shared memory is illustrated via the simple example of a matrix multiplication $C = AB$ for the case with $A$ of dimension $M \times w$, $B$ of dimension $w \times N$, and $C$ of dimension $M \times N$. To keep the kernels simple, $M$ and $N$ are multiples of 32, and $w$ is 16 for devices of compute capability 1.x or 32 for devices of compute capability 2.x.

A natural decomposition of the problem is to use a block and tile size of $w \times w$ threads. Therefore, in terms of $w \times w$ tiles, $A$ is a column matrix, $B$ is a row matrix, and $C$ is their outer product; see Figure 6.9. A grid of $N/w$ by $M/w$ blocks is launched, where each
thread block calculates the elements of a different tile in C from a single tile of A and a single tile of B.

![Diagram showing matrix multiplication](image)

**Figure 6.9** Block-column matrix (A) multiplied by block-row matrix (B) with resulting product matrix (C)

To do this, the `simpleMultiply` kernel (Listing 6.8) calculates the output elements of a tile of matrix C.

```c
__global__ void simpleMultiply(float *a, float* b, float *c, int N)
{
    int row = blockIdx.y * blockDim.y + threadIdx.y;
    int col = blockIdx.x * blockDim.x + threadIdx.x;
    float sum = 0.0f;
    for (int i = 0; i < TILE_DIM; i++) {
        sum += a[row*TILE_DIM+i] * b[i*N+col];
    }
    c[row*N+col] = sum;
}
```

**Listing 6.8 Unoptimized matrix multiplication**

In Listing 6.8, `a`, `b`, and `c` are pointers to global memory for the matrices A, B, and C, respectively; `blockDim.x`, `blockDim.y`, and `TILE_DIM` are all equal to `w`. Each thread in the `w×w`-thread block calculates one element in a tile of C. `row` and `col` are the row and column of the element in C being calculated by a particular thread. The `for` loop over `i` multiplies a row of A by a column of B, which is then written to C.

The effective bandwidth of this kernel is only 14.5GB/s on an NVIDIA Tesla M2090 (with ECC on). To analyze performance, it is necessary to consider how warps access global
Memory Optimizations

memory in the for loop. Each warp of threads calculates one row of a tile of C, which depends on a single row of A and an entire tile of B as illustrated in Figure 6.10.

![Diagram of matrix multiplication]

Figure 6.10 Computing a row of a tile in C using one row of A and an entire tile of B

For each iteration i of the for loop, the threads in a warp read a row of the B tile, which is a sequential and coalesced access for all compute capabilities.

However, for each iteration i, all threads in a warp read the same value from global memory for matrix A, as the index row*TILE_DIM+i is constant within a warp. Even though such an access requires only 1 transaction on devices of compute capability 2.x, there is wasted bandwidth in the transaction, because only one 4-byte word out of 32 words in the cache line is used. We can reuse this cache line in subsequent iterations of the loop, and we would eventually utilize all 32 words; however, when many warps execute on the same multiprocessor simultaneously, as is generally the case, the cache line may easily be evicted from the cache between iterations i and i+1.

The performance on a device of any compute capability can be improved by reading a tile of A into shared memory as shown in Listing 6.9.

```c
__global__ void coalescedMultiply(float *a, float *b, float *c, int N)
{
    __shared__ float aTile[TILE_DIM][TILE_DIM];

    int row = blockIdx.y * blockDim.y + threadIdx.y;
    int col = blockIdx.x * blockDim.x + threadIdx.x;
    float sum = 0.0f;
    aTile[threadIdx.y][threadIdx.x] = a[row*TILE_DIM+threadIdx.x];

    for (int i = 0; i < N; i++)
    {
        float bRow = b[row*TILE_DIM+i];
        float cRow = c[row*TILE_DIM+i];
        for (int j = 0; j < TILE_DIM; j++)
        {
            aTile[threadIdx.y][threadIdx.x] += aTile[threadIdx.y][j] * bRow;
        }
        c[row*TILE_DIM+i] = cRow + aTile[threadIdx.y][threadIdx.x];
    }
}
```
### Listing 6.9 Using shared memory to improve the global memory load efficiency in matrix multiplication

In Listing 6.9, each element in a tile of A is read from global memory only once, in a fully coalesced fashion (with no wasted bandwidth), to shared memory. Within each iteration of the for loop, a value in shared memory is broadcast to all threads in a warp. No __syncthreads() synchronization barrier call is needed after reading the tile of A into shared memory because only threads within the warp that write the data into shared memory read the data (Note: in lieu of __syncthreads(), the __shared__ array may need to be marked as volatile for correctness on devices of compute capability 2.x; see the NVIDIA Fermi Compatibility Guide). This kernel has an effective bandwidth of 32.7GB/s on an NVIDIA Tesla M2090. This illustrates the use of the shared memory as a “user-managed cache” when the hardware L1 cache eviction policy does not match up well with the needs of the application.

A further improvement can be made to how Listing 6.9 deals with matrix B. In calculating each of the rows of a tile of matrix C, the entire tile of B is read. The repeated reading of the B tile can be eliminated by reading it into shared memory once (Listing 6.10).

#### Listing 6.10 Improvement by reading additional data into shared memory

Note that in Listing 6.10, a __syncthreads() call is required after reading the B tile because a warp reads data from shared memory that were written to shared memory by different warps. The effective bandwidth of this routine is 38.7 GB/s on an NVIDIA Tesla.
M2090. Note that the performance improvement is not due to improved coalescing in either case, but to avoiding redundant transfers from global memory.

The results of the various optimizations are summarized in Table 6.2.

<table>
<thead>
<tr>
<th>Optimization</th>
<th>NVIDIA Tesla M2090</th>
</tr>
</thead>
<tbody>
<tr>
<td>No optimization</td>
<td>14.5 GB/s</td>
</tr>
<tr>
<td>Coalesced using shared memory to store a tile of A</td>
<td>32.7 GB/s</td>
</tr>
<tr>
<td>Using shared memory to eliminate redundant reads of a tile of B</td>
<td>38.7 GB/s</td>
</tr>
</tbody>
</table>

Table 6.2  Performance Improvements Optimizing C = AB Matrix Multiply

Medium Priority: Use shared memory to avoid redundant transfers from global memory.

6.2.2.3  Shared Memory in Matrix Multiplication (C = AAᵀ)

A variant of the previous matrix multiplication can be used to illustrate how strided accesses to global memory, as well as shared memory bank conflicts, are handled. This variant simply uses the transpose of A in place of B, so C = AAᵀ.

A simple implementation for C = AAᵀ is shown in Listing 6.11.

```c
__global__ void simpleMultiply(float *a, float *c, int M)
{
    int row = blockIdx.y * blockDim.y + threadIdx.y;
    int col = blockIdx.x * blockDim.x + threadIdx.x;
    float sum = 0.0f;
    for (int i = 0; i < TILE_DIM; i++) {
        sum += a[row*TILE_DIM+i] * a[col*TILE_DIM+i];
    }
    c[row*M+col] = sum;
}
```

Listing 6.11 Unoptimized handling of strided accesses to global memory

In Listing 6.11, the row-th, col-th element of C is obtained by taking the dot product of the row-th and col-th rows of A. The effective bandwidth for this kernel is 3.64 GB/s on an NVIDIA Tesla M2090. These results are substantially lower than the corresponding measurements for the C = AB kernel. The difference is in how threads in a half warp access elements of A in the second term, a[col*TILE_DIM+i], for each iteration i. For a warp of threads, col represents sequential columns of the transpose of A, and therefore
`col*TILE_DIM` represents a strided access of global memory with a stride of `w`, resulting in plenty of wasted bandwidth.

The way to avoid strided access is to use shared memory as before, except in this case a warp reads a row of `A` into a column of a shared memory tile, as shown in Listing 6.12.

```c
__global__ void coalescedMultiply(float *a, float *c, int M) {
    __shared__ float aTile[TILE_DIM][TILE_DIM],
                   transposedTile[TILE_DIM][TILE_DIM];
    int row = blockIdx.y * blockDim.y + threadIdx.y;
    int col = blockIdx.x * blockDim.x + threadIdx.x;
    float sum = 0.0f;
    aTile[threadIdx.y][threadIdx.x] = a[row*TILE_DIM+threadIdx.x];
    transposedTile[threadIdx.x][threadIdx.y] =
            a[(blockIdx.x*blockDim.x + threadIdx.y)*TILE_DIM +
              threadIdx.x];
    __syncthreads();
    for (int i = 0; i < TILE_DIM; i++) {
        sum += aTile[threadIdx.y][i]* transposedTile[i][threadIdx.x];
    }
    c[row*M+col] = sum;
}
```

Listing 6.12 An optimized version of Listing 6.11 using coalesced reads from global memory

Listing 6.12 uses the shared `transposedTile` to avoid uncoalesced accesses in the second term in the dot product and the shared `aTile` technique from the previous example to avoid uncoalesced accesses in the first term. The effective bandwidth of this kernel is 27.5 GB/s on an NVIDIA Tesla M2090. These results are slightly lower than those obtained by the final kernel for `C = AB`. The cause of the difference is shared memory bank conflicts.

The reads of elements in `transposedTile` within the `for` loop are free of conflicts, because threads of each half warp read across rows of the tile, resulting in unit stride across the banks. However, bank conflicts occur when copying the tile from global memory into shared memory. To enable the loads from global memory to be coalesced, data are read from global memory sequentially. However, this requires writing to shared memory in columns, and because of the use of `w×w` tiles in shared memory, this results in a stride between threads of `w` banks — every thread of the warp hits the same bank. (Recall that `w` is selected as 16 for devices of compute capability 1.x and 32 for devices of compute capability 2.x.) These many-way bank conflicts are very expensive. The simple remedy is to pad the shared memory array so that it has an extra column, as in the following line of code.

```c
__shared__ float transposedTile[TILE_DIM][TILE_DIM+1];
```
This padding eliminates the conflicts entirely, because now the stride between threads is \( w+1 \) banks (i.e., 17 or 33, depending on the compute capability), which, due to modulo arithmetic used to compute bank indices, is equivalent to a unit stride. After this change, the effective bandwidth is 39.2 GB/s on an NVIDIA Tesla M2090, which is comparable to the results from the last \( C = AB \) kernel.

The results of these optimizations are summarized in Table 6.3.

<table>
<thead>
<tr>
<th>Optimization</th>
<th>NVIDIA Tesla M2090</th>
</tr>
</thead>
<tbody>
<tr>
<td>No optimization</td>
<td>3.6 GB/s</td>
</tr>
<tr>
<td>Using shared memory to coalesce global reads</td>
<td>27.5 GB/s</td>
</tr>
<tr>
<td>Removing bank conflicts</td>
<td>39.2 GB/s</td>
</tr>
</tbody>
</table>

Table 6.3  Performance Improvements Optimizing \( C = AA^T \) Matrix Multiplication

These results should be compared with those in Table 6.2. As can be seen from these tables, judicious use of shared memory can dramatically improve performance.

The examples in this section have illustrated three reasons to use shared memory:

- To enable coalesced accesses to global memory, especially to avoid large strides (for general matrices, strides are much larger than 32)
- To eliminate (or reduce) redundant loads from global memory
- To avoid wasted bandwidth

### 6.2.3 Local Memory

Local memory is so named because its scope is local to the thread, not because of its physical location. In fact, local memory is off-chip. Hence, access to local memory is as expensive as access to global memory. Like global memory, local memory is not cached on devices of compute capability 1.x. In other words, the term “local” in the name does not imply faster access.

Local memory is used only to hold automatic variables. This is done by the `nvcc` compiler when it determines that there is insufficient register space to hold the variable. Automatic variables that are likely to be placed in local memory are large structures or arrays that would consume too much register space and arrays that the compiler determines may be indexed dynamically.

Inspection of the PTX assembly code (obtained by compiling with `-ptx` or `-keep` command-line options to `nvcc`) reveals whether a variable has been placed in local memory during the first compilation phases. If it has, it will be declared using the `.local` mnemonic and accessed using the `ld.local` and `st.local` mnemonics. If it has not,
subsequent compilation phases might still decide otherwise, if they find the variable consumes too much register space for the targeted architecture. There is no way to check this for a specific variable, but the compiler reports total local memory usage per kernel (lmem) when run with the --ptxas-options=-v option.

6.2.4 Texture Memory

The read-only texture memory space is cached. Therefore, a texture fetch costs one device memory read only on a cache miss; otherwise, it just costs one read from the texture cache. The texture cache is optimized for 2D spatial locality, so threads of the same warp that read texture addresses that are close together will achieve best performance. Texture memory is also designed for streaming fetches with a constant latency; that is, a cache hit reduces DRAM bandwidth demand, but not fetch latency.

In certain addressing situations, reading device memory through texture fetching can be an advantageous alternative to reading device memory from global or constant memory.

6.2.4.1 Additional Texture Capabilities

If textures are fetched using tex1D(), tex2D(), or tex3D() rather than tex1Dfetch(), the hardware provides other capabilities that might be useful for some applications such as image processing, as shown in Table 6.4.

<table>
<thead>
<tr>
<th>Feature</th>
<th>Use</th>
<th>Caveat</th>
</tr>
</thead>
<tbody>
<tr>
<td>Filtering</td>
<td>Fast, low-precision interpolation between texels</td>
<td>Valid only if the texture reference returns floating-point data</td>
</tr>
<tr>
<td>Normalized texture coordinates</td>
<td>Resolution-independent coding</td>
<td></td>
</tr>
<tr>
<td>Addressing modes</td>
<td>Automatic handling of boundary cases¹</td>
<td>Can be used only with normalized texture coordinates</td>
</tr>
</tbody>
</table>

Table 6.4 Useful Features for tex1D(), tex2D(), and tex3D() Fetches

¹The automatic handling of boundary cases in the bottom row of Table 6.4 refers to how a texture coordinate is resolved when it falls outside the valid addressing range. There are two options: clamp and wrap. If \( x \) is the coordinate and \( N \) is the number of texels for a one-dimensional texture, then with clamp, \( x \) is replaced by 0 if \( x < 0 \) and by \( 1 - 1/N \) if \( 1 \leq x \). With wrap, \( x \) is replaced by \( \text{frac}(x) \) where \( \text{frac}(x) = x - \text{floor}(x) \). Floor returns the largest integer less than or equal to \( x \). So, in clamp mode where \( N = 1 \), an \( x \) of 1.3 is clamped to 1.0; whereas in wrap mode, it is converted to 0.3

Within a kernel call, the texture cache is not kept coherent with respect to global memory writes, so texture fetches from addresses that have been written via global stores in the same kernel call return undefined data. That is, a thread can safely read a memory location via texture if the location has been updated by a previous kernel call or memory copy, but not if it has been previously updated by the same thread or another
thread within the same kernel call. This is relevant only when fetching from linear or pitch-linear memory because a kernel cannot write to CUDA arrays.

### 6.2.5 Constant Memory

There is a total of 64 KB constant memory on a device. The constant memory space is cached. As a result, a read from constant memory costs one memory read from device memory only on a cache miss; otherwise, it just costs one read from the constant cache.

For all threads of a half warp, reading from the constant cache is as fast as reading from a register as long as all threads read the same address. Accesses to different addresses by threads within a half warp are serialized, so cost scales linearly with the number of different addresses read by all threads within a half warp.

Alternatively, on devices of compute capability 2.x, programs use the Load Uniform (LDU) operation; see Section F.4.4 of the CUDA C Programming Guide for details.

### 6.2.6 Registers

Generally, accessing a register consumes zero extra clock cycles per instruction, but delays may occur due to register read-after-write dependencies and register memory bank conflicts.

The latency of read-after-write dependencies is approximately 24 cycles, but this latency is completely hidden on multiprocessors that have at least 192 active threads (that is, 6 warps) for devices of compute capability 1.x (8 CUDA cores per multiprocessor * 24 cycles of latency = 192 active threads to cover that latency). For devices of compute capability 2.0, which have 32 CUDA cores per multiprocessor, as many as 768 threads might be required to completely hide latency.

The compiler and hardware thread scheduler will schedule instructions as optimally as possible to avoid register memory bank conflicts. They achieve the best results when the number of threads per block is a multiple of 64. Other than following this rule, an application has no direct control over these bank conflicts. In particular, there is no register-related reason to pack data into float4 or int4 types.

#### 6.2.6.1 Register Pressure

Register pressure occurs when there are not enough registers available for a given task. Even though each multiprocessor contains thousands of 32-bit registers (see Section F.1 of the CUDA C Programming Guide), these are partitioned among concurrent threads. To prevent the compiler from allocating too many registers, use the -maxrregcount=N compiler command-line option (see Section B.1 below) or the launch bounds kernel definition qualifier (see Section B.17 of the CUDA C Programming Guide) to control the maximum number of registers to allocated per thread.
6.3 ALLOCATION

Device memory allocation and de-allocation via `cudaMalloc()` and `cudaFree()` are expensive operations, so device memory should be reused and/or sub-allocated by the application wherever possible to minimize the impact of allocations on overall performance.
Chapter 7.
EXECUTION CONFIGURATION OPTIMIZATIONS

One of the keys to good performance is to keep the multiprocessors on the device as busy as possible. A device in which work is poorly balanced across the multiprocessors will deliver suboptimal performance. Hence, it’s important to design your application to use threads and blocks in a way that maximizes hardware utilization and to limit practices that impede the free distribution of work. A key concept in this effort is occupancy, which is explained in the following sections.

Another important concept is the management of system resources allocated for a particular task. How to manage this resource utilization is discussed in the final sections of this chapter.

7.1 OCCUPANCY

Thread instructions are executed sequentially in CUDA, and, as a result, executing other warps when one warp is paused or stalled is the only way to hide latencies and keep the hardware busy. Some metric related to the number of active warps on a multiprocessor is therefore important in determining how effectively the hardware is kept busy. This metric is occupancy.

Occupancy is the ratio of the number of active warps per multiprocessor to the maximum number of possible active warps. (To determine the latter number, see the deviceQuery code sample in the GPU Computing SDK or refer to Appendix F in the CUDA C Programming Guide.) Another way to view occupancy is the percentage of the hardware’s ability to process warps that is actively in use.
Higher occupancy does not always equate to higher performance—there is a point above which additional occupancy does not improve performance. However, low occupancy always interferes with the ability to hide memory latency, resulting in performance degradation.

### 7.1.1 Calculating Occupancy

One of several factors that determine occupancy is register availability. Register storage enables threads to keep local variables nearby for low-latency access. However, the set of registers (known as the register file) is a limited commodity that all threads resident on a multiprocessor must share. Registers are allocated to an entire block all at once. So, if each thread block uses many registers, the number of thread blocks that can be resident on a multiprocessor is reduced, thereby lowering the occupancy of the multiprocessor. The maximum number of registers per thread can be set manually at compilation time per-file using the `--maxrregcount` option or per-kernel using the `__launch_bounds__` qualifier (see Section 6.2.6.1).

For purposes of calculating occupancy, the number of registers used by each thread is one of the key factors. For example, devices with compute capability 1.0 and 1.1 have 8,192 32-bit registers per multiprocessor and can have a maximum of 768 simultaneous threads resident (24 warps x 32 threads per warp). This means that in one of these devices, for a multiprocessor to have 100% occupancy, each thread can use at most 10 registers. However, this approach of determining how register count affects occupancy does not take into account the register allocation granularity. For example, on a device of compute capability 1.0, a kernel with 128-thread blocks using 12 registers per thread results in an occupancy of 83% with 5 active 128-thread blocks per multiprocessor, whereas a kernel with 256-thread blocks using the same 12 registers per thread results in an occupancy of 66% because only two 256-thread blocks can reside on a multiprocessor.

Furthermore, register allocations are rounded up to the nearest 256 registers per block on devices with compute capability 1.0 and 1.1.

The number of registers available, the maximum number of simultaneous threads resident on each multiprocessor, and the register allocation granularity vary over different compute capabilities. Because of these nuances in register allocation and the fact that a multiprocessor’s shared memory is also partitioned between resident thread blocks, the exact relationship between register usage and occupancy can be difficult to determine. The `--ptxas-options=-v` option of `nvcc` details the number of registers used per thread for each kernel. See Section 4.2 of the *CUDA C Programming Guide* for the register allocation formulas for devices of various compute capabilities and Section F.1 of the programming guide for the total number of registers available on those devices. Alternatively, NVIDIA provides an occupancy calculator in the form of an Excel spreadsheet that enables developers to hone in on the optimal balance and to test different possible scenarios more easily. This spreadsheet, shown in Using the CUDA Occupancy Calculator Usage to project GPU multiprocessor occupancy, is called...
CUDA_Occupancy_Calculator.xls and is located in the tools subdirectory of the CUDA Toolkit installation.

Figure 7.1 Using the CUDA Occupancy Calculator Usage to project GPU multiprocessor occupancy

In addition to the calculator spreadsheet, occupancy can be determined using the NVIDIA Visual Profiler's Achieved Occupancy metric. The Visual Profiler also calculates occupancy as part of the Multiprocessor stage of application analysis.

7.2 HIDING REGISTER DEPENDENCIES

**Medium Priority**: To hide latency arising from register dependencies, maintain sufficient numbers of active threads per multiprocessor (i.e., sufficient occupancy).

Register dependencies arise when an instruction uses a result stored in a register written by an instruction before it. The latency on current CUDA-enabled GPUs is approximately 24 cycles, so threads must wait 24 cycles before using an arithmetic
result. However, this latency can be completely hidden by the execution of threads in other warps. See Section 6.2.6 for details.

7.3 THREAD AND BLOCK HEURISTICS

**Medium Priority:** The number of threads per block should be a multiple of 32 threads, because this provides optimal computing efficiency and facilitates coalescing.

The dimension and size of blocks per grid and the dimension and size of threads per block are both important factors. The multidimensional aspect of these parameters allows easier mapping of multidimensional problems to CUDA and does not play a role in performance. As a result, this section discusses size but not dimension.

Latency hiding and occupancy depend on the number of active warps per multiprocessor, which is implicitly determined by the execution parameters along with resource (register and shared memory) constraints. Choosing execution parameters is a matter of striking a balance between latency hiding (occupancy) and resource utilization.

Choosing the execution configuration parameters should be done in tandem; however, there are certain heuristics that apply to each parameter individually. When choosing the first execution configuration parameter—the number of blocks per grid, or grid size—the primary concern is keeping the entire GPU busy. The number of blocks in a grid should be larger than the number of multiprocessors so that all multiprocessors have at least one block to execute. Furthermore, there should be multiple active blocks per multiprocessor so that blocks that aren’t waiting for a __syncthreads() can keep the hardware busy. This recommendation is subject to resource availability; therefore, it should be determined in the context of the second execution parameter—the number of threads per block, or block size—as well as shared memory usage. To scale to future devices, the number of blocks per kernel launch should be in the thousands.

When choosing the block size, it is important to remember that multiple concurrent blocks can reside on a multiprocessor, so occupancy is not determined by block size alone. In particular, a larger block size does not imply a higher occupancy. For example, on a device of compute capability 1.1 or lower, a kernel with a maximum block size of 512 threads results in an occupancy of 66 percent because the maximum number of threads per multiprocessor on such a device is 768. Hence, only a single block can be active per multiprocessor. However, a kernel with 256 threads per block on such a device can result in 100 percent occupancy with three resident active blocks.
As mentioned in Section 7.1, higher occupancy does not always equate to better performance. For example, improving occupancy from 66 percent to 100 percent generally does not translate to a similar increase in performance. A lower occupancy kernel will have more registers available per thread than a higher occupancy kernel, which may result in less register spilling to local memory. Typically, once an occupancy of 50 percent has been reached, additional increases in occupancy do not translate into improved performance. It is in some cases possible to fully cover latency with even fewer warps, notably via instruction-level parallelism (ILP); for discussion, see http://www.nvidia.com/content/GTC-2010/pdfs/2238_GTC2010.pdf.

There are many such factors involved in selecting block size, and inevitably some experimentation is required. However, a few rules of thumb should be followed:

- Threads per block should be a multiple of warp size to avoid wasting computation on under-populated warps and to facilitate coalescing.
- A minimum of 64 threads per block should be used, and only if there are multiple concurrent blocks per multiprocessor.
- Between 128 and 256 threads per block is a better choice and a good initial range for experimentation with different block sizes.
- Use several (3 to 4) smaller thread blocks rather than one large thread block per multiprocessor if latency affects performance. This is particularly beneficial to kernels that frequently call __syncthreads().

Note that when a thread block allocates more registers than are available on a multiprocessor, the kernel launch fails, as it will when too much shared memory or too many threads are requested.

### 7.4 EFFECTS OF SHARED MEMORY

Shared memory can be helpful in several situations, such as helping to coalesce or eliminate redundant access to global memory. However, it also can act as a constraint on occupancy. In many cases, the amount of shared memory required by a kernel is related to the block size that was chosen, but the mapping of threads to shared memory elements does not need to be one-to-one. For example, it may be desirable to use a 32×32 element shared memory array in a kernel, but because the maximum number of threads per block is 512, it is not possible to launch a kernel with 32×32 threads per block. In such cases, kernels with 32×16 or 32×8 threads can be launched with each thread processing two or four elements, respectively, of the shared memory array. The approach of using a single thread to process multiple elements of a shared memory array can be beneficial even if limits such as threads per block are not an issue. This is because some operations common to each element can be performed by the thread once, amortizing the cost over the number of shared memory elements processed by the thread.
A useful technique to determine the sensitivity of performance to occupancy is through experimentation with the amount of dynamically allocated shared memory, as specified in the third parameter of the execution configuration. By simply increasing this parameter (without modifying the kernel), it is possible to effectively reduce the occupancy of the kernel and measure its effect on performance.

As mentioned in the previous section, once an occupancy of more than 50 percent has been reached, it generally does not pay to optimize parameters to obtain higher occupancy ratios. The previous technique can be used to determine whether such a plateau has been reached.
Chapter 8.
INSTRUCTION OPTIMIZATIONS

Awareness of how instructions are executed often permits low-level optimizations that can be useful, especially in code that is run frequently (the so-called hot spot in a program). Best practices suggest that this optimization be performed after all higher-level optimizations have been completed.

8.1 ARITHMETIC INSTRUCTIONS

Single-precision floats provide the best performance, and their use is highly encouraged.

The throughput of individual arithmetic operations on devices of compute capability 1.x is detailed in Section F.3 of the CUDA C Programming Guide, and the throughput of these operations on devices of compute capability 2.x is detailed in Section F.4 of the programming guide.

8.1.1 Division and Modulo Operations

Low Priority: Use shift operations to avoid expensive division and modulo calculations.

Integer division and modulo operations are particularly costly and should be avoided or replaced with bitwise operations whenever possible: If \( n \) is a power of 2, \( (i/n) \) is equivalent to \( i \gg \log_2(n) \) and \( i \% n \) is equivalent to \( i \& (n-1) \).

The compiler will perform these conversions if \( n \) is literal. (For further information, refer to Chapter 5 of the CUDA C Programming Guide).
8.1.2  Reciprocal Square Root

The reciprocal square root should always be invoked explicitly as `rsqrtf()` for single precision and `rsqrt()` for double precision. The compiler optimizes $1.0f/\sqrt{f(x)}$ into `rsqrtf()` only when this does not violate IEEE-754 semantics.

8.1.3  Other Arithmetic Instructions

- **Low Priority:** Avoid automatic conversion of doubles to floats.

  The compiler must on occasion insert conversion instructions, introducing additional execution cycles. This is the case for

  - Functions operating on `char` or `short` whose operands generally need to be converted to an `int`
  - Double-precision floating-point constants (defined without any type suffix) used as input to single-precision floating-point computations

  The latter case can be avoided by using single-precision floating-point constants, defined with an `f` suffix such as `3.141592653589793f`, `1.0f`, `0.5f`. This suffix has accuracy implications in addition to its ramifications on performance. The effects on accuracy are discussed in Section 4.3.3. Note that this distinction is particularly important to performance on devices of compute capability 2.x.

  For single-precision code, use of the `float` type and the single-precision math functions are highly recommended. When compiling for devices without native double-precision support such as devices of compute capability 1.2 and earlier, each double-precision floating-point variable is converted to single-precision floating-point format (but retains its size of 64 bits) and double-precision arithmetic is demoted to single-precision arithmetic.

  It should also be noted that the CUDA math library’s complementary error function, `erfcf()`, is particularly fast with full single-precision accuracy.

8.1.4  Math Libraries

- **Medium Priority:** Use the fast math library whenever speed trumps precision.

  Two types of runtime math operations are supported. They can be distinguished by their names: some have names with prepended underscores, whereas others do not (e.g., `__functionName()` versus `functionName()`). Functions following the `__functionName()` naming convention map directly to the hardware level. They are faster but provide somewhat lower accuracy (e.g., `__sinf(x)` and `__expf(x)`). Functions following `functionName()` naming convention are slower but have higher accuracy (e.g., `sinf(x)`
and \( \text{expf}(x) \)). The throughput of \( \_\text{sinf}(x), \_\text{cosf}(x), \text{and} \_\text{expf}(x) \) is much greater than that of \( \text{sinf}(x), \text{cosf}(x), \text{and tanf}(x) \). The latter become even more expensive (about an order of magnitude slower) if the magnitude of the argument \( x \) needs to be reduced. Moreover, in such cases, the argument-reduction code uses local memory, which can affect performance even more because of the high latency of local memory. More details are available in the CUDA C Programming Guide.

Note also that whenever sine and cosine of the same argument are computed, the \text{sincos} family of instructions should be used to optimize performance:

- \text{sincosf()} for single-precision fast math (see next paragraph)
- \text{sincosf()} for regular single-precision
- \text{sincos()} for double precision

The \text{-use_fast_math} compiler option of \text{nvcc} coerces every functionName() call to the equivalent \text{__functionName()} call. This switch should be used whenever accuracy is a lesser priority than the performance. This is frequently the case with transcendental functions. Note this switch is effective only on single-precision floating point.

**Medium Priority: Prefer faster, more specialized math functions over slower, more general ones when possible.**

For small integer powers (e.g., \( x^2 \) or \( x^3 \)), explicit multiplication is almost certainly faster than the use of general exponentiation routines such as \text{pow()}. While compiler optimization improvements continually seek to narrow this gap, explicit multiplication (or the use of an equivalent purpose-built inline function or macro) can have a significant advantage. This advantage is increased when several powers of the same base are needed (e.g., where both \( x^2 \) and \( x^5 \) are calculated in close proximity), as this aids the compiler in its common sub-expression elimination (CSE) optimization.

For exponentiation using base 2 or 10, use the functions \text{exp2()} or \text{exp2f()} and \text{exp10()} or \text{exp10f()} rather than the functions \text{pow()} or \text{powf()}. Both \text{pow()} and \text{powf()} are heavy-weight functions in terms of register pressure and instruction count due to the numerous special cases arising in general exponentiation and the difficulty of achieving good accuracy across the entire ranges of the base and the exponent. The functions \text{exp2()}, \text{exp2f()}, \text{exp10()}, and \text{exp10f()}, on the other hand, are similar to \text{exp()} and \text{expf()} in terms of performance, and can be as much as ten times faster than their \text{pow()}/\text{powf()} equivalents.

For exponentiation with an exponent of \( 1/3 \), use the \text{cbrt()} or \text{cbrtf()} function rather than the generic exponentiation functions \text{pow()} or \text{powf()}, as the former are significantly faster than the latter. Likewise, for exponentiation with an exponent of \(-1/3\), use \text{rcbrt()} or \text{rcbrtf()}.

Replace \( \sin(\pi*<\text{expr}>) \) with \text{sinpi(<expr>)} and \( \cos(\pi*<\text{expr}>) \) with \text{cospi(<expr>)}. This is advantageous with regard to both accuracy and performance. As a particular example,
to evaluate the sine function in degrees instead of radians, use sinpi(x/180.0).
Similarly, the single-precision functions sinpif() and cospif() should replace calls to
sinf() and cosf() when the function argument is of the form π*<expr>. (The
performance advantage sinpi() has over sin() is due to simplified argument reduction;
the accuracy advantage is because sinpi() multiplies by π only implicitly, effectively
using an infinitely precise mathematical π rather than a single- or double-precision
approximation thereof.)

8.1.5 Precision-related Compiler Flags

By default, the nvcc compiler generates IEEE-compliant code for devices of compute
capability 2.x, but it also provides options to generate code that somewhat less accurate
but faster and that is closer to the code generated for earlier devices:

- -ftz=true (denormalized numbers are flushed to zero)
- -prec-div=false (less precise division)
- -prec-sqrt=false (less precise square root)

Another, more aggressive, option is -use_fast_math, which coerces every
functionName() call to the equivalent __functionName() call. This makes the code run
faster at the cost of diminished precision and accuracy. See Section 8.1.4.

8.2 MEMORY INSTRUCTIONS

High Priority: Minimize the use of global memory. Prefer shared memory access
where possible.

Memory instructions include any instruction that reads from or writes to shared, local,
or global memory. When accessing uncached local or global memory, there are 400 to
600 clock cycles of memory latency.

As an example, the assignment operator in the following sample code has a high
throughput, but, crucially, there is a latency of 400 to 600 clock cycles to read data from
global memory:

```c
__shared__ float shared[32];
__device__ float device[32];
shared[threadIdx.x] = device[threadIdx.x];
```

Much of this global memory latency can be hidden by the thread scheduler if there are
sufficient independent arithmetic instructions that can be issued while waiting for the
global memory access to complete. However, it is best to avoid accessing global memory
whenever possible.
Chapter 9.
CONTROL FLOW

9.1 BRANCHING AND DIVERGENCE

**High Priority: Avoid different execution paths within the same warp.**

Any flow control instruction (if, switch, do, for, while) can significantly affect the
instruction throughput by causing threads of the same warp to diverge; that is, to follow
different execution paths. If this happens, the different execution paths must be
serialized, since all of the threads of a warp share a program counter; this increases the
total number of instructions executed for this warp. When all the different execution
paths have completed, the threads converge back to the same execution path.

To obtain best performance in cases where the control flow depends on the thread ID,
the controlling condition should be written so as to minimize the number of divergent
warps.

This is possible because the distribution of the warps across the block is deterministic as
mentioned in Section 4.1 of the CUDA C Programming Guide. A trivial example is when
the controlling condition depends only on \((\text{threadIdx} / \text{WSIZE})\) where \(\text{WSIZE}\) is the warp
size.

In this case, no warp diverges because the controlling condition is perfectly aligned with
the warps.
9.2 BRANCH PREDICATION

Low Priority: Make it easy for the compiler to use branch predication in lieu of loops or control statements.

Sometimes, the compiler may unroll loops or optimize out `if` or `switch` statements by using branch predication instead. In these cases, no warp can ever diverge. The programmer can also control loop unrolling using

```c
#pragma unroll
```

For more information on this pragma, refer to the CUDA C Programming Guide.

When using branch predication, none of the instructions whose execution depends on the controlling condition is skipped. Instead, each such instruction is associated with a per-thread condition code or predicate that is set to true or false according to the controlling condition. Although each of these instructions is scheduled for execution, only the instructions with a true predicate are actually executed. Instructions with a false predicate do not write results, and they also do not evaluate addresses or read operands.

The compiler replaces a branch instruction with predicated instructions only if the number of instructions controlled by the branch condition is less than or equal to a certain threshold: If the compiler determines that the condition is likely to produce many divergent warps, this threshold is 7; otherwise it is 4.

9.3 LOOP COUNTERS SIGNED VS. UNSIGNED

Medium Priority: Use signed integers rather than unsigned integers as loop counters.

In the C language standard, unsigned integer overflow semantics are well defined, whereas signed integer overflow causes undefined results. Therefore, the compiler can optimize more aggressively with signed arithmetic than it can with unsigned arithmetic. This is of particular note with loop counters: since it is common for loop counters to have values that are always positive, it may be tempting to declare the counters as unsigned. For slightly better performance, however, they should instead be declared as signed.

For example, consider the following code:

```c
for (i = 0; i < n; i++) {
    out[i] = in[offset + stride*i];
}
```
Here, the sub-expression \( \text{stride} \times i \) could overflow a 32-bit integer, so if \( i \) is declared as unsigned, the overflow semantics prevent the compiler from using some optimizations that might otherwise have applied, such as strength reduction. If instead \( i \) is declared as signed, where the overflow semantics are undefined, the compiler has more leeway to use these optimizations.
Having completed the GPU acceleration of one or more components of the application it is possible to compare the outcome with the original expectation. Recall that the initial assess step allowed the developer to determine an upper bound for the potential speedup attainable by accelerating given hotspots.

Before tackling other hotspots to improve the total speedup, the developer should consider taking the partially parallelized implementation and carry it through to production. This is important for a number of reasons; for example, it allows the user to profit from their investment as early as possible (the speedup may be partial but is still valuable), and it minimizes risk for the developer and the user by providing an evolutionary rather than revolutionary set of changes to the application.
With each generation of NVIDIA processors, new features are added to the GPU that CUDA can leverage. Consequently, it’s important to understand the characteristics of the architecture.

Programmers should be aware of two version numbers. The first is the compute capability, and the second is the version number of the CUDA Runtime and CUDA Driver APIs.

10.1 CUDA COMPUTE CAPABILITY

The compute capability describes the features of the hardware and reflects the set of instructions supported by the device as well as other specifications, such as the maximum number of threads per block and the number of registers per multiprocessor. Higher compute capability versions are supersets of lower (that is, earlier) versions, so they are backward compatible.

The compute capability of the GPU in the device can be queried programmatically as illustrated in the NVIDIA GPU Computing SDK in the deviceQuery sample. The output for that program is shown in Figure 10.1. This information is obtained by calling cudaGetDeviceProperties() and accessing the information in the structure it returns.
Figure 10.1 Sample CUDA configuration data reported by deviceQuery

The major and minor revision numbers of the compute capability are shown on the third and fourth lines of Figure 10.1. Device 0 of this system has compute capability 1.1.

More details about the compute capabilities of various GPUs are in Appendices A and F of the CUDA C Programming Guide. In particular, developers should note the number of multiprocessors on the device, the number of registers and the amount of memory available, and any special capabilities of the device.

10.2 ADDITIONAL HARDWARE DATA

Certain hardware features are not described by the compute capability. For example, the ability to overlap kernel execution with asynchronous data transfers between the host and the device is available on most but not all GPUs with compute capability 1.1. In such cases, call `cudaGetDeviceProperties()` to determine whether the device is capable of a certain feature. For example, the `deviceOverlap` field of the device property structure indicates whether overlapping kernel execution and data transfers is possible (displayed in the “Concurrent copy and execution” line of Figure 10.1); likewise, the `canMapHostMemory` field indicates whether zero-copy data transfers can be performed.

10.3 CUDA RUNTIME AND DRIVER API VERSION

The CUDA Driver API and the CUDA Runtime are two of the programming interfaces to CUDA. Their version number enables developers to check the features associated with these APIs and decide whether an application requires a newer (later) version than
the one currently installed. This is important because the CUDA Driver API is *backward compatible but not forward compatible*, meaning that applications, plug-ins, and libraries (including the CUDA Runtime) compiled against a particular version of the Driver API will continue to work on subsequent (later) driver releases. However, applications, plug-ins, and libraries (including the CUDA Runtime) compiled against a particular version of the Driver API may not work on earlier versions of the driver, as illustrated in Figure 10.2.

**Figure 10.2 Compatibility of CUDA versions**

### 10.4 WHICH COMPUTE CAPABILITY TO TARGET

When in doubt about the compute capability of the hardware that will be present at runtime, it is best to assume a compute capability of 1.0 as defined in the *CUDA C Programming Guide*, Section F.1, or a compute capability of 1.3 if double-precision arithmetic is required.

To target specific versions of NVIDIA hardware and CUDA software, use the `--arch`, `--code`, and `--gencode` options of `nvcc`. Code that contains double-precision arithmetic, for example, must be compiled with `"--arch=sm_13"` (or higher compute capability), otherwise double-precision arithmetic will get demoted to single-precision arithmetic (see Section 4.3.3). This and other compiler switches are discussed further in Appendix B.
10.5 CUDA RUNTIME

The host runtime component of the CUDA software environment can be used only by host functions. It provides functions to handle the following:

- Device management
- Context management
- Memory management
- Code module management
- Execution control
- Texture reference management
- Interoperability with OpenGL and Direct3D

As compared to the lower-level CUDA Driver API, the CUDA Runtime greatly eases device management by providing implicit initialization, context management, and device code module management. The C/C++ host code generated by nvcc utilizes the CUDA Runtime, so applications that link to this code will depend on the CUDA Runtime; similarly, any code that uses the cuBLAS, cuFFT, and other CUDA Toolkit libraries will also depend on the CUDA Runtime, which is used internally by these libraries.

The functions that make up the CUDA Runtime API are explained in the *CUDA Toolkit Reference Manual*.

The CUDA Runtime handles kernel loading and setting up kernel parameters and launch configuration before the kernel is launched. The implicit driver version checking, code initialization, CUDA context management, CUDA module management (cubin to function mapping), kernel configuration, and parameter passing are all performed by the CUDA Runtime.

It comprises two principal parts:

- A C-style function interface (*cuda_runtime_api.h*).
- C++-style convenience wrappers (*cuda_runtime.h*) built on top of the C-style functions.

For more information on the Runtime API, refer to Section 3.2 of the *CUDA C Programming Guide*. 

11.1 ERROR HANDLING

All CUDA Runtime API calls return an error code of type `cudaError_t`; the return value will be equal to `cudaSuccess` if no errors have occurred. (The exceptions to this are kernel launches, which return `void`, and `cudaGetErrorString()`, which returns a character string describing the `cudaError_t` code that was passed into it.) The CUDA Toolkit libraries (cuBLAS, cuFFT, etc.) likewise return their own sets of error codes.

Since some CUDA API calls and all kernel launches are asynchronous with respect to the host code, errors may be reported to the host asynchronously as well; often this occurs the next time the host and device synchronize with each other, such as during a call to `cudaMemcpy()` or to `cudaDeviceSynchronize()`.

Always check the error return values on all CUDA API functions, even for functions that are not expected to fail, as this will allow the application to detect and recover from errors as soon as possible should they occur. Applications that do not check for CUDA API errors could at times run to completion without having noticed that the data calculated by the GPU is incomplete, invalid, or uninitialized.

11.2 DISTRIBUTING THE CUDA RUNTIME AND LIBRARIES

The CUDA Toolkit’s end-user license agreement (EULA) allows for redistribution of many of the CUDA libraries under certain terms and conditions.
This allows applications that depend on these libraries to redistribute the exact versions of the libraries against which they were built and tested, thereby avoiding any trouble for end users who might have a different version of the CUDA Toolkit (or perhaps none at all) installed on their machines.

Please refer to the EULA for details.

Note: this does not apply to the NVIDIA driver; the end user must still download and install an NVIDIA driver appropriate to their GPU(s) and operating system.
Chapter 12.
DEPLOYMENT INFRASTRUCTURE TOOLS

12.1 NVIDIA-SMI

The NVIDIA System Management Interface (nvidia-smi) is a command line utility that aids in the management and monitoring of NVIDIA GPU devices. This utility allows administrators to query GPU device state and, with the appropriate privileges, permits administrators to modify GPU device state. nvidia-smi is targeted at Tesla and certain Quadro GPUs, though limited support is also available on other NVIDIA GPUs. nvidia-smi ships with NVIDIA GPU display drivers on Linux, and with 64-bit Windows Server 2008 R2 and Windows 7. nvidia-smi can output queried information as XML or as human-readable plain text either to standard output or to a file. See the nvidia-smi documentation for details. Please note that new versions of nvidia-smi are not guaranteed to be backward-compatible with previous versions.

12.1.1 Queryable state

- **ECC error counts.** Both correctable single-bit and detectable double-bit errors are reported. Error counts are provided for both the current boot cycle and the lifetime of the GPU.
- **GPU utilization.** Current utilization rates are reported for both the compute resources of the GPU and the memory interface.
- **Active compute process.** The list of active processes running on the GPU is reported, along with the corresponding process name/ID and allocated GPU memory.
- **Clocks and performance state.** Max and current clock rates are reported for several important clock domains, as well as the current GPU performance state (pstate).
- **Temperature and fan speed.** The current GPU core temperature is reported, along with fan speeds for products with active cooling.
Power management. The current board power draw and power limits are reported for products that report these measurements.

Identification. Various dynamic and static information is reported, including board serial numbers, PCI device IDs, VBIOS/Inforom version numbers and product names.

12.1.2 Modifiable state

- **ECC mode.** Enable and disable ECC reporting.
- **ECC reset.** Clear single- and double-bit ECC error counts.
- **Compute mode.** Indicate whether compute processes can run on the GPU and whether they run exclusively or concurrently with other compute processes.
- **Persistence mode.** Indicate whether the NVIDIA driver stays loaded when no applications are connected to the GPU. It is best to enable this option in most circumstances.
- **GPU reset.** Reinitialize the GPU hardware and software state via a secondary bus reset.

12.2 NVML

The NVIDIA Management Library (NVML) is a C-based interface that provides direct access to the queries and commands exposed via nvidia-smi intended as a platform for building 3rd-party system management applications. The NVML API is available on the NVIDIA developer website as part of the Tesla Deployment Kit through a single header file and is accompanied by PDF documentation, stub libraries, and sample applications; see [http://developer.nvidia.com/tesla-deployment-kit](http://developer.nvidia.com/tesla-deployment-kit). Each new version of NVML is backward-compatible.

An additional set of Perl and Python bindings are provided for the NVML API. These bindings expose the same features as the C-based interface and also provide backwards compatibility. The Perl bindings are provided via CPAN and the Python bindings via PyPI.

All of these products (nvidia-smi, NVML, and the NVML language bindings) are updated with each new CUDA release and provide roughly the same functionality.

12.3 CLUSTER MANAGEMENT TOOLS

Managing your GPU cluster will help achieve maximum GPU utilization and help you and your users extract the best possible performance. Many of the industry’s most popular cluster management tools now support CUDA GPUs via NVML. For a listing of some of these tools, see http://developer.nvidia.com/cluster-management.

12.4 COMPILER JIT CACHE MANAGEMENT

Any PTX device code loaded by an application at runtime is compiled further to binary code by the device driver. This is called just-in-time compilation (JIT). Just-in-time compilation increases application load time but allows applications to benefit from latest compiler improvements. It is also the only way for applications to run on devices that did not exist at the time the application was compiled.

When JIT compilation of PTX device code is used, the NVIDIA driver caches the resulting binary code on disk. Some aspects of this behavior such as cache location and maximum cache size can be controlled via the use of environment variables; see Section 3.1.1.2 of the CUDA C Programming Guide.

12.5 CUDA_VISIBLE_DEVICES

It is possible to rearrange the collection of installed CUDA devices that will visible to and enumerated by a CUDA application prior to the start of that application by way of the CUDA_VISIBLE_DEVICES environment variable.

Devices to be made visible to the application should be included as a comma-separated list in terms of the system-wide list of enumerable devices. For example, to use only devices 0 and 2 from the system-wide list of devices, set CUDA_VISIBLE_DEVICES=0,2 before launching the application. The application will then enumerate these devices as device 0 and device 1, respectively.
Appendix A.
RECOMMENDATIONS AND BEST PRACTICES

This appendix contains a summary of the recommendations for optimization that are explained in this document.

A.1 Overall Performance Optimization Strategies

Performance optimization revolves around three basic strategies:

- Maximizing parallel execution
- Optimizing memory usage to achieve maximum memory bandwidth
- Optimizing instruction usage to achieve maximum instruction throughput

Maximizing parallel execution starts with structuring the algorithm in a way that exposes as much data parallelism as possible. Once the parallelism of the algorithm has been exposed, it needs to be mapped to the hardware as efficiently as possible. This is done by carefully choosing the execution configuration of each kernel launch. The application should also maximize parallel execution at a higher level by explicitly exposing concurrent execution on the device through streams, as well as maximizing concurrent execution between the host and the device.

Optimizing memory usage starts with minimizing data transfers between the host and the device because those transfers have much lower bandwidth than internal device data transfers. Kernel access to global memory also should be minimized by maximizing the use of shared memory on the device. Sometimes, the best optimization might even be to avoid any data transfer in the first place by simply recomputing the data whenever it is needed.
The effective bandwidth can vary by an order of magnitude depending on the access pattern for each type of memory. The next step in optimizing memory usage is therefore to organize memory accesses according to the optimal memory access patterns. This optimization is especially important for global memory accesses, because latency of access costs hundreds of clock cycles. Shared memory accesses, in counterpoint, are usually worth optimizing only when there exists a high degree of bank conflicts.

As for optimizing instruction usage, the use of arithmetic instructions that have low throughput should be avoided. This suggests trading precision for speed when it does not affect the end result, such as using intrinsics instead of regular functions or single precision instead of double precision. Finally, particular attention must be paid to control flow instructions due to the SIMT (single instruction multiple thread) nature of the device.
Appendix B. NVCC COMPILER SWITCHES

B.1 NVCC

The NVIDIA \texttt{nvcc} compiler driver converts .cu files into C for the host system and CUDA assembly or binary instructions for the device. It supports a number of command-line parameters, of which the following are especially useful for optimization and related best practices:

- \texttt{-arch=sm\_13} or higher is required for double precision. See Section 4.3.3.
- \texttt{-maxrregcount=N} specifies the maximum number of registers kernels can use at a per-file level. See Section 6.2.6.1. (See also the \texttt{__launch_bounds__} qualifier discussed in Section B.17 of the CUDA C Programming Guide to control the number of registers used on a per-kernel basis.)
- \texttt{--ptxas-options=-v} or \texttt{-Xptxas=-v} lists per-kernel register, shared, and constant memory usage.
- \texttt{-ftz=true} (denormalized numbers are flushed to zero)
- \texttt{-prec-div=false} (less precise division)
- \texttt{-prec-sqrt=false} (less precise square root)
- \texttt{-use\_fast\_math} compiler option of \texttt{nvcc} coerces every \texttt{functionName()} call to the equivalent \texttt{__functionName()} call. This makes the code run faster at the cost of diminished precision and accuracy. See Section 8.1.4.
Appendix C.
REVISION HISTORY

C.1 Version 4.1

- Rearranged the entire guide based on the Assess, Parallelize, Optimize, Deploy pattern.
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